<u>Unit Title</u>: Unit 1: Transformations/Geometric Sequences/ Pythagorean Theorem (41 Days)

Stage 1: Desired Results

Standards & Indicators: Major:

8.G.1 Verify experimentally the properties of rotations, reflections, and translations.

- a. Lines are taken to lines, and line segments to line segments of the same length.
- b. Angles are taken to angles of the same measure.
- c. Parallel lines are taken to parallel lines.

8.G.2 Understand that a two-dimensional figure is congruent to another if the second can be obtained from the first by a sequence of rotations, reflections, and translations; given two congruent figures, describe a sequence that exhibits the congruence between them.

8.G.3 Describe the effect of dilations, translations, rotations, and reflections on two-dimensional figures using coordinates.

8.G.4 Understand that a two-dimensional figure is similar to another if the second can be obtained from the first by a sequence of rotations, reflections, translations, and dilations; given two similar two-dimensional figures, describe a sequence that exhibits the similarity between them

8.G.5 Use informal arguments to establish facts about the angle sum and exterior angle of triangles, about the angles created when parallel lines are cut by a transversal, and the angle-angle criterion for similarity of triangles. For example, arrange three copies of the same triangle so that the sum of the three angles appears to form a line, and give an argument in terms of transversals why this is so.

Mathematical Practices

MP.1 Make sense of problems and persevere in solving them

MP. 2 Reason abstractly and quantitatively

- MP.3 Construct viable arguments and critique the reasoning of others
- MP. 4 Model with mathematics

MP. 5 Use appropriate tools strategically

MP. 6 Attend to precision

MP. 7 Look for and make use of structure

MP. 8 Look for and express regularity in repeated reasoning

| Career Readiness, Life Literacies and Key Skills | | | |
|--|--|---|--|
| Standard | Performance Expectations | Core Ideas | |
| 9.4.12.CI.1 | Demonstrate the ability to reflect, analyze, and use creative skills and ideas (e.g., 1.1.12 prof.CR3a). | With a growth mindset, failure is an important part of success. | |
| 9.4.12.CT.1 | Identify problem-solving strategies used in the development of an innovative product or practice (e.g., 1.1.12acc.C1b, | Collaboration with individuals with diverse experiences can aid in the problem-solving process, | |

| | 2.2.12.PF.3). | | particularly for global issues where | |
|--|--|--|--|--|
| 9.4.12.CT.2 | Explain the potential benefits of | | diverse solutions are needed. | |
| | collaborating to enhance critical thinking | | | |
| | and problem solving | (e.g., | | |
| | 1.3E.12profCR3.a). | | | |
| 9.4.12.TL.1 | Assess digital tools based on features such as accessibility options, capacities, and utility for accomplishing a specific task (e.g., W.11-12.6.). | | Digital tools differ in features, capacities, and styles. Knowledge of different digital tools is helpful in selecting the best tool for a | |
| | | | given task. | |
| 9.4.8.TL.3 | Select appropriate tools to organize and present information digitally. | | Some digital tools are appropriate for gathering, organizing, analyzing, and presenting information, while other types of digital tools are appropriate for creating text, visualizations, models, and communicating with others. | |
| Central Idea/Enduring Un | derstanding: | Essential/Guiding Que | estion: | |
| Chapter 5 | | At the end of the Unit | t, students should be able to answer | |
| Parallel lines are lines in | the same plane which | the Essential Questions: | | |
| never intersect. A line that | t intersects two or | Chapter 5: 1. How are the measures of angles related when | | |
| more lines is called a tran | sversal. I riangles are | | | |
| their number of congruent sides. A polygon is | | parallel lines are cut by a transversal? | | |
| a closed figure formed by | t slues. A polygoli is | 2. How can you use the Pythagorean Theorem to find | | |
| segments Polygons are classified by their | | the distance be | etween two points on the coordinate | |
| number of sides. An examination of the | | plane? | | |
| number of triangles that r | nake up each kind of | Chapter 6: | | |
| polygon shows that the su | Im S of the interior | | | |
| angles of any polygon can be found by | | 1. How are figur | es translated on the coordinate | |
| subtracting 2 from the number of sides n and | | plane? | | |
| multiplying by 180. The Pythagorean Theorem | | 2. How are dilati | ons similar to scale drawings? | |
| describes the relationship between the legs and | | Chantor 7: | | |
| the hypotenuse for any right triangle. | | 1. Why do translations, reflections, and rotations | | |
| Chanter 6 | | create congrue | ent images? | |
| Δ transformation is an operation that maps an | | 2. How is the slo | pe of a line related to the similar | |
| original geometric figure, the pre-image, onto | | slope triangles | s formed by the line? | |
| a new figure called the image. A reflection is a | | | | |
| transformation produced by flipping a figure | | | | |
| over the line of symmetry. A rotation is a | | | | |
| transformation produced by turning a figure | | | | |
| about a fixed point called the center of | | | | |
| rotation.A dilation is a transformation | | | | |

| produced by enlarging or reducing an original figure by a scale factor. | |
|---|---|
| Chapter 7 In two congruent figures, you can determine the transformation, or series of transformations, that maps one figure onto the other by analyzing the orientation or relative position of the figures.Similar figures have the same shape, but may have different sizes. The sizes of the two figures are related to the scale factor of the dilation <u>Content: Chapters 5-7 (Course 3)</u> | Skills(Objectives): |
| Lesson 5.1 Understanding Lines Lesson 5.2 Understanding and Writing Geometric Proofs Lesson 5.3 Angles of Triangles Lesson 5.4 Angles of Polygons Lesson 5.5 Pythagorean Theorem Lesson 5.6 Using the Pythagorean Theorem Lesson 5.7 Finding Distances on the Coordinate Graph Lesson 6.1 Translation Lesson 6.2 Rotations Lesson 6.3 Reflections Lesson 6.3 Reflections Lesson 6.4 Dilations Lesson 7.1 Congruence and Transformations Lesson 7.2 Congruence Lesson 7.3 Similarity and Transformations Lesson 7.4 Properties of Similar Polygons Lesson 7.5 Similar Triangles and Indirect Measures Lesson 7.6 Slope and Similar Triangles Lesson 7.7 Area and Perimeter of Similar Polygons | Identity the legs and hypotenuse of a right triangle. Investigate and generalize the relationship between the areas of the squares created using the side lengths of a triangle. Generalize an informal justification of the Pythagorean Theorem and its converse. Use the Pythagorean Theorem to determine if a triangle is a right triangle. Use the Pythagorean Theorem to find a missing side length of a right triangle. Plot right triangles on a coordinate plane to investigate the relationship of side lengths. Recognize that the distance between two coordinate points can be the length of the hypotenuse of a right triangle. Apply the Pythagorean Theorem to find the distance between two points in the coordinate plane, Model real-world problems including lengths that cannot be directly measured. Use a variety of resources including physical models, transparencies, or geometry software to explore transformations to verify their properties using examples both with and without coordinates. Discover that rotations, reflections, and translations preserve angle measures and side lengths. |

| Discover that dilations only preserve angle measure whereas corresponding side lengths are proportional. Explore the relationships between the coordinates of figures before and after transformations. Describe the effect of transformations on two-dimensional figures using coordinates. Given two similar figures, describe a sequence of transformations that demonstrates the similarity hot work. |
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| between them using examples both with and without coordinates. |
| Investigate the sum of the interior angles of a triangle using physical models or geometry software. |
| • Explore the angle relationship between an exterior angle and the two remote interior angles of the triangle. |
| • Investigate relationships of pairs of angles created by parallel lines cut by a transversal using |
| transformations. |

Interdisciplinary Connections:

Interdisciplinary connections are integrated in each unit with connections to the mathematical practices.

Stage 2: Assessment Evidence

| <u>Performance Task(s)</u> : | Other Evidence: | |
|---|---|--|
| 8.EE.B.6: Slopes Between Points on a Line | Online and Written Assignments | |
| 8.F.A.3: Introduction to Linear Functions | Mid Chapter Quizzes | |
| 8.F.B.4: <u>Baseball Cards</u> | End of Chapter Assessments | |
| 8.F.B.4: Video Streaming | End of Unit Common Assessments | |
| 8.EE.C.8c: <u>Summer Swimming</u> | | |
| 8.EE.C.8: Cell Phone Plans | | |
| 8.EE.C.8: Kimi and Jordan | | |
| 8.EE.C.8a: The Intersection of Two Lines | | |
| 8.F.A.1: Function Rules | | |
| 8.F.A.1: Introducing Functions | | |
| 8.F.A.2: Battery Charging | | |
| Stage 3: Learning Plan | | |
| Learning Opportunities/Strategies: | Resources: | |
| Use various Think-Pair-Share strategies | Glencoe Math Course 3 Textbook (Chapters 5-7) | |
| provided by Glencoe for each lesson. | IXL | |
| | Kahoot | |
| Lesson 5.1 Understanding Lines-classify the | Khan Academy | |
| angles formed and find missing angles when | Lesson Presentations | |
| parallel lines are cut by a transversal. | Graphing Calculator | |

| | Google Forms and Sheets | | |
|---|--|--|--|
| Lesson 5.2 Understanding and Writing | ALEKS | | |
| Geometric Proofs-use definitions, properties, | Gimkit | | |
| and theorems to prove a hypothesis | Google apps for education | | |
| | Desmos | | |
| Lesson 5.3 Angles of Triangles-find missing | Woot Math | | |
| angle measures in triangles. | Quizizz | | |
| | Quizalize | | |
| Lesson 5.4 Angles of Polygons-find the | Flocabulary | | |
| measures of angles in polygons | Brain Pop | | |
| | Mash-Up Math | | |
| Lesson 5.5 Pythagorean Theorem-use the | Easel by Teachers Pay Teachers | | |
| Pythagorean Theorem and it converse to solve | Classkick | | |
| problems. | Edulastic | | |
| | Math Literacy | | |
| Lesson 5.6 Using the Pythagorean | • I can solve a word problem <u>graphic organizer</u> | | |
| Theorem-use the Pythagorean Theorem to | • Think pair share <u>graphic organizer</u> | | |
| solve problems | • Vocabulary <u>Word Map</u> | | |
| | • <u>Frayer Model</u> | | |
| Lesson 5.7 Finding Distances on the | • Collection of <u>Graphic Organizers</u> | | |
| Coordinate Graph-find the distance between | LGBT and Disabilities Resources: | | |
| two points on a coordinate plane | • <u>LGBTQ-Inclusive Lesson & Resources by Garden</u> | | |
| | State Equality and Make it Better for Youth | | |
| Lesson 6.1 Translation - graph translations on | • LGBTQ+ BOOKS | | |
| the coordinate plane | • Inclusive Math Class | | |
| Lasson (2) Detetions should notations on the | DEI Resources: | | |
| Lesson 0.2 Rotations-graph rotations on the | • <u>Learning for Justice</u> CLSEN Educator Descurress | | |
| coordinate plane | <u>OLSEN Educator Resources</u> Supporting L CPTOLA Youth Passauros List | | |
| | <u>Supporting LOBTQIA Toutil Resource List</u> Despect Ability: Fighting Stigmes, Advensing | | |
| | • <u>Respect Ability: Fighting Stigmas, Advancing</u> Opportunities | | |
| | NIDOF Diversity Equity & Inclusion Educational | | |
| | Resources | | |
| | Diversity Calendar | | |
| Differentiation *Please note: Teachers who have | students with 504 plans that require curricular | | |

Differentiation *Please note: Teachers who have students with 504 plans that require curricular accommodations are to refer to Struggling and/or Special Needs Section for differentiation

| High-Achieving Students | On Grade Level Students | Struggling Students | Special Needs/ELL |
|----------------------------|----------------------------|-------------------------|---------------------------------------|
| Khan Academy | Tutoring | Provide a highly | Any student requiring further |
| Project based learning | Tables | structured, predictable | accommodations and/or modifications |
| Tablets | Graphic organizers | learning environment | will have them individually listed in |
| Challenging problems | Differentiation of | Provide | their 504 Plan or IEP. These might |
| with higher degree of | learning strategies: | organizers/study | include, but are not limited to: |
| difficulty | visual, auditory, | guides | breaking assignments into smaller |
| Higher order thinking | kinetic and | | tasks, giving directions through |

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Unit Title: Unit 2: Volume & Surface Area, Real Numbers, Scientific Notation, Exponents (40 Days)

Stage 1: Desired Results

<u>Standards & Indicators</u>: Major:

8.G.9 Know the formulas for the volumes of cones, cylinders, and spheres and use them to solve real-world and mathematical problems.

8.EE.1-Use scientific notation to estimate and express the values of very large or very small numbers and compare their values (how many times larger/smaller is one than the other).

8.EE.A.2b Simplify numerical radicals, limiting to square roots (i.e. nonperfect squares). For example, simplify $\sqrt{8}$ to $2\sqrt{2}$.

8.EE.3-Perform operations using numbers expressed in scientific notation, including problems where both decimals and scientific notation are used (interpret scientific notation generated when technology has been used for calculations).

8.EE.4-In real-world problem solving situations choose units of appropriate size for measurement of very small and very large quantities.

8.NS.1- Compare rational and irrational numbers to demonstrate that the decimal expansion of irrational numbers do not repeat; show that every rational number has a decimal expansion which eventually repeats and convert such decimals into rational numbers. Use rational numbers to approximate and locate irrational numbers on a number line and estimate the value of expressions involving irrational numbers.

8.NS.2- Apply the properties of integer exponents to simplify and write equivalent numerical expressions.

8.NS.A.3 Understand that the sum or product of two rational numbers is rational; that the sum of a rational number and an irrational number is irrational; and that the product of a nonzero rational number and an irrational number is irrational

Integration of Climate Change

8.G.C.9 Know the formulas for the volumes of cones, cylinders, and spheres and use them to solve real-world and mathematical problems. Z
 Climate Change Example: Students may use the formula for the volume of a sphere to approximate the volume of hailstones to consider how climate change may affect the size of hailstones over time.

Mathematical Practices

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- MP. 2 Reason abstractly and quantitatively
- MP.3 Construct viable arguments and critique the reasoning of others
- MP. 4 Model with mathematics
- MP. 5 Use appropriate tools strategically
- MP. 6 Attend to precision
- MP. 7 Look for and make use of structure

MP. 8 Look for and express regularity in repeated reasoning

| Career Readiness, Life Literacies and Key Skills | | | |
|--|--|--|--|
| Standard | Performance Expectations | Core Ideas | |
| 9.4.12.CI.1 | Demonstrate the ability to reflect, analyze, and use creative skills and ideas (e.g., 1.1.12 prof.CR3a). | With a growth mindset, failure is an important part of success. | |
| 9.4.12.CT.1 | Identify problem-solving strategies used in the development of an innovative product or practice (e.g., 1.1.12acc.C1b, 2.2.12.PF.3). | Collaboration with individuals with diverse experiences can aid in the problem-solving process, particularly for global issues where | |
| 9.4.12.CT.2 | Explain the potential benefits of collaborating to enhance critical thinking and problem solving (e.g., 1.3E.12profCR3.a). | diverse solutions are needed. | |
| 9.4.12.TL.1 | Assess digital tools based on features such as accessibility options, capacities, and utility for accomplishing a specific task (e.g., W.11-12.6.). | Digital tools differ in features, capacities, and styles. Knowledge of different digital tools is helpful in selecting the best tool for a given task. | |
| 9.4.8.TL.3 | Select appropriate tools to organize and present information digitally. | Some digital tools are appropriate for gathering, organizing, analyzing, and presenting information, while other types of | |

| | | | | digital tools are appropriate for |
|--|-------------------------|---------|------------------|---|
| | | | | creating text, visualizations, |
| | | | | models, and communicating with |
| | | | | others. |
| Central Idea/Enduring Und | lerstanding: | Essent | tial/Guiding Que | estion: |
| <u>Chapter 8:</u> | | Chapt | er 8: Why are | formulas important in math and |
| Lessons 1-3: Volume is the | e measure of space | scienc | e? | |
| occupied by a three-dimen | nsional region. It is | 1. | How is the for | mula for the volume of a cylinder to |
| measured in cubic units. | | | the formula for | r the volume of a rectangular prism? |
| Lessons 4-6 : The lateral a | rea of a prism is the | 2. | What would have | ave a greater effect on the volume of |
| sum of the areas of the lat | eral faces. The | | a cone: doublin | ng its radius or doubling its height? |
| surface area is the sum of | the lateral area and | 3. | True or False: | The volume of a sphere is $\frac{2}{3}$ the |
| the area of the base(s). Sin | milar solids are 3D | | volume of a cy | linder with the same radius r and |
| figures that have the same | e shape and whose | | height of 2r? | |
| corresponding linear meas | sures are | 4. | How is a calcu | lation affected if you round n to |
| proportional. The scale fa | ctor of similar solids | | 3.14 or use the | e pi key on your calculator? |
| is how much larger or sma | aller one solid is than | 5. | How does the | volume of a three dimensional |
| another. It is written as a n | atio in simplest | | figure differ fr | rom its surface area? |
| form. | | 6. | How is the vol | lume of a prism affected when its |
| | | | dimensions are | e tripled? |
| <u>Chapter 1</u> : | | | | |
| Lesson 1: Rational number | ers are numbers that | Chapt | er 1: Why is it | helpful to write numbers in |
| can be written as fractions | s. Both terminating | differe | ent ways? | - |
| and repeating decimals ca | n be written as | 1. | How can you o | determine if a number is a rational |
| fractions, but non-terminating, non-repeating | | | number? | |
| numbers such as | | 2. | How can I wri | te repeated multiplication using |
| π and $\sqrt{2}$ cannot be written | as fractions. So | | powers? | |
| these numbers are not rati | onal. The rules and | 3. | How can I use | the properties of integer exponents |
| properties for adding sub | tracting multiplying | | to simplify alg | ebraic and numeric expressions? |
| and dividing rational num | hers are the same as | 4. | How does the | Product of Powers law apply to |
| those for integers and frac | tions | | finding the po | wer of a power? |
| Lossons 2 4: A product of reported factors can | | 5. | How are negat | tive exponents and positive |
| be expressed as a power 1 | ising an exponent | | exponents rela | ted? |
| and a base. From this defi | nition comes the | 6. | Why would I r | need to use square roots and cube |
| Laws and Exponents whi | ch include: Product | | roots? | 1 |
| of Powers Quotient of Po | wers Power of a | 7. | How can I esti | mate the square root of a |
| Power and Power of a Product | | | non-perfect sq | uare? |
| Lesson 5: By definition | ny nonzero number | 8. | How are real r | numbers different from irrational |
| to the zero power is 1 and any nonzero number | | | numbers? | |
| to a negative power, n, is the multiplicative | | | | |
| inverse of its nth power. | | | | |
| Lessons 8-10: Squaring a number and finding | | | | |
| a square root are inverse operations. Cubing a | | | | |
| number and finding a cube are inverse | | | | |
| operations | | | | |
| operations. | | | | |

| Content: | Skills(Objectives): | | |
|---|---|--|--|
| <u>Chapter 8</u> : | <u>Chapter 8</u> : | | |
| 8.1: Volume of Cylinders | 8.1: Find the volume of cylinders. | | |
| 8.2: Volume of Cones | 8.2: Find the volume of cones. | | |
| 8.3: Volume of Spheres | 8.3: Find the volume of spheres. | | |
| 8.4: Surface Area of Cylinders | 8.4: Find the surface area of cylinders. | | |
| 8.5: Surface Area of Cones | 8.5: Find the surface area of cones. | | |
| 8.6: Changes in Dimensions | 8.6: Solve problems involving similar solids. | | |
| | | | |
| <u>Chapter 1</u> : | <u>Chapter 1</u> : | | |
| Lesson 1.1 Rational Numbers | 1.1 Identify Rational Numbers | | |
| Lesson 1.2 Exponents and Powers | 1.2 Write and Evaluate Powers | | |
| Lesson 1.3 Multiply & Divide Monomials | 1.3 Product and Quotient of Powers | | |
| Lesson 1.4 Powers of Exponents | 1.4 Evaluate Powers of Exponents | | |
| Lesson 1.5 Negative Exponents | 1.5 Write Negative Exponents as Positive and Simplify | | |
| Lesson 1.6 Scientific Notation | 1.6 Write Large or Small Numbers in Scientific Notation | | |
| Lesson 1.7 Compute with Scientific Notation | 1.7 Multiply, Divide, Add and Subtract Numbers in | | |
| Lesson 1.8 Roots | Scientific Notation | | |
| Lesson 1.9 Estimate of Roots | 1.8 Find Square and Cube Roots | | |
| Lesson 1.10 Comparing Real Numbers | 1.9 Estimate Square Roots of Non-Perfect Squares | | |
| | 1.10 Compare Real Numbers in Various Formats | | |

Interdisciplinary Connections:

Interdisciplinary connections are integrated in each unit with connections to the mathematical practices.

| Stage 2: Assessment Evidence | | | |
|---|---|--|--|
| Performance Task(s): | Other Evidence: | | |
| 8.G.9-Glasses | Online and Written Assignments | | |
| https://www.illustrativemathematics.org/conte | Mid Chapter Quizzes | | |
| nt-standards/8/G/C/9/tasks/112 | End of Chapter Assessments | | |
| | End of Unit Common Assessments | | |
| 8.NS.A.1: Identifying Rational Numbers | | | |
| 8.NS.A.1: <u>Repeating or Terminating</u> | | | |
| 8.NS.A.2: Placing a Square Root on the | | | |
| Number Line | | | |
| 8.NS.A.2: Comparing Rational and Irrational | | | |
| Numbers | | | |
| 8.NS.A.1: Representations of Rational | | | |
| Numbers to Fraction Representations | | | |
| Stage 3 | : Learning Plan | | |
| Learning Opportunities/Strategies: | Resources: | | |
| Use various Think-Pair-Share strategies | Glencoe Math Course 3 Textbook (Chapters 5-7) | | |
| provided by Glencoe for each lesson. | IXL | | |
| Lesson 8.1: Have students work with a partner | Kahoot | | |
| to complete two exercises. Have them use the | Khan Academy | | |

| following template to find the volume of each | Lesson Presentations |
|--|---|
| cylinder: volume=area of base x height of | Graphing Calculator |
| cylinder. If they are still struggling, have them | Google Forms and Sheets |
| replace area of base with pi x r x r. | ALEKS |
| Lesson 8.2: Have students work in small | Gimkit |
| groups to complete 5 exercises. Provide each | Google apps for education |
| student with 6 chips. Each student must place | Desmos |
| a chip in the center of the table after | Woot Math |
| contributing to the discussion. After all of their | Quizizz |
| chips are gone, they may no longer talk and all | Quizalize |
| students must use all of their chips. | Flocabulary |
| Lesson 8.3: Have pairs complete the graphic | Brain Pon |
| organizer. Have them come up with as many | Mash-Un Math |
| real world examples of spheres as possible or | Easel by Teachers Pay Teachers |
| objects that are approximately spheres | Classkick |
| Lesson 8.4: Have students work in a small | Edulastic |
| group to complete 4 exercises Each student is | Math Literacy |
| responsible for leading the discussion for one | • I can solve a word problem graphic organizer |
| of the exercises. | Think pair share graphic organizer |
| Lesson 8.5: Have students work in teams. | Vocabulary Word Map |
| Each student writes down two facts and one | • Fraver Model |
| fib about the surface area of volume of a cone. | Collection of Graphic Organizers |
| The job of the team is to identify the fib. | LGBT and Disabilities Resources: |
| Lesson 8.6: Have students work with a partner | LGBTO-Inclusive Lesson & Resources by Garden |
| to write a real world problem involving two | State Equality and Make it Better for Youth |
| similar solids. Have them trade problems with | • LGBTO+ Books |
| another pair of students to solve each other's | • Inclusive Math Class |
| problem. | DEI Resources: |
| 1 | • Learning for Justice |
| Lesson 1.1: Make up sets of index cards with | GLSEN Educator Resources |
| different types of number sets, such as odd and | • Supporting LGBTOIA Youth Resource List |
| even, fractions, and decimals. Each set of | • Respect Ability: Fighting Stigmas, Advancing |
| cards should have 10-20 different numbers. | Opportunities |
| Divide students into small groups and give | NJDOE Diversity, Equity & Inclusion Educational |
| each group a set of cards. Ask them to classify | Resources |
| each number in as many ways as you can. | • Diversity Calendar |
| Lesson 1.2: Have students work in a group to | |
| make and complete a table similar to the one | |
| shown using a factor other than 3. | |
| Lesson 1.3: Have students work in pairs to | |
| complete the Enrich worksheet. Have them | |
| trade their solutions with another pair of | |
| students and discuss any differences. | |
| Lesson 1.4: Remind students how to find the | |
| volume of a cube. First have them write the | |

| side length three times. Then, have them | |
|---|--|
| rewrite the expression without exponents. | |
| Finally, have them write the expression using | |
| only one base and one exponent. | |
| Lesson 1.5: Think-Pair-Share: Ask students: | |
| How is 100 written as a power of 10? 1,000? | |
| Lesson 1.8: Ask students if it matters whether | |
| the factors are both positive or both negative | |
| when dealing with perfect squares. | |
| Lesson 1.9: Designate a leader to call out each | |
| of the following numbers one at a time: 100, 9, | |
| 36, 64, 49, 4, 25, 81, and 16. Ask students to | |
| hold up the square root of the number using | |
| their fingers. | |
| Lesson 1.10: First give each member of the | |
| pair two index cards and have them write the | |
| definition of rational numbers and give some | |
| examples on one card. Then ask them to write | |
| a definition of irrational numbers based on | |
| their definition or rational numbers. Have | |
| them share with a partner to verify their | |
| definitions. | |
| | |

Differentiation *Please note: Teachers who have students with 504 plans that require curricular accommodations are to refer to Struggling and/or Special Needs Section for differentiation

| accommodations are to refer to Strugging and/or special Needs Section for unreferituation | | | | |
|---|------------------------|-------------------------|---------------------------------------|--|
| High-Achieving | On Grade Level | Struggling Students | Special Needs/ELL | |
| Students | Students | | | |
| Khan Academy | Tutoring | Provide a highly | Any student requiring further | |
| Project based learning | Tables | structured, predictable | accommodations and/or modifications | |
| Tablets | Graphic organizers | learning environment | will have them individually listed in | |
| Challenging problems | Differentiation of | Provide | their 504 Plan or IEP. These might | |
| with higher degree of | learning strategies: | organizers/study | include, but are not limited to: | |
| difficulty | visual, auditory, | guides | breaking assignments into smaller | |
| Higher order thinking | kinetic and | Lessons designed to | tasks, giving directions through | |
| questions | cooperative | the style of learning | several channels (auditory, visual, | |
| Differentiation of pacing | Technology | that matches the | kinesthetic, model), and/or small | |
| and activities | connection | student | group instruction for reading/writing | |
| Differentiation of learning | Practice Assignments | Cooperative Learning | | |
| strategies: visual, | Puzzle time activities | Positive | ELL supports should include, but are | |
| auditory, kinetic and | Record and practice | reinforcement | not limited to, the following:: | |
| cooperative | journal | Announce test with | Extended time | |
| Enrichment and extension | Differentiating the | adequate prep time | Provide visual aids | |
| Technology connection | lesson activities | Lessons presentation | Repeated directions | |
| Practice assignments | Lesson tutorials | available on google | Differentiate based on proficiency | |
| Puzzle time activities | Skills review | classroom | Provide word banks | |
| Record and practice | handbook | Frequent check for | Allow for translators, dictionaries | |
| journal | | understanding | | |

| Break down task into manageable units One-on-one instruction Tutoring Pair student with a |
|--|
| Pair student with a high achieving student |

Unit Title: Unit 3: Equations with One and Two Variables & Functions

Stage 1: Desired Results

Standards & Indicators:

8.EE.C.7a: Give examples of linear equations in one variable with one solution, infinitely many solutions, or no solutions. Show which of these possibilities is the case by successively transforming given equation into simpler forms until an equivalent equation of the form x = a, a = a, or a = b results (where a and b are different numbers).

8.EE.C.7b: Solve linear equations with rational number coefficients, including equations whose solutions require expanding expressions using the distributive property and collecting like terms.

8.EE.B.5: Graph proportional relationships, interpreting the unit rate as the slope of the graph. Compare two different proportional relationships represented in different ways.

8.EE.B.6: Use similar triangles to explain why the slope m is the same between any two distinct points on a non-vertical line in the coordinate plane; derive the equation y = mx for a line through the origin and the equation y = mx + b for a line intercepting the vertical axis at b.

8.F.A.2: Compare properties of two functions each represented in a different way (algebraically, graphically, numerically in tables, or by verbal descriptions).

8.F.B.4: Construct a function to model a linear relationship between two quantities. Determine the rate of change and initial value of the function from a description of a relationship or from two (x,y) values, including reading these from a table or from a graph. Interpret the rate of change and initial value of a linear function in terms of the situation it models, and in terms of its graph or a table of values.

8.F.A.3: Interpret the equation y=mx+b as defining a linear function, whose graph is a straight line; give examples of functions that are not linear.

8.EE.C.8c: Solve real-world and mathematical problems leading to two linear equations in two variables.

8.EE.C.8: Analyze and solve pairs of simultaneous linear equations.

8.EE.C.8a: Understand that solutions to a system of two linear equations in two variables correspond to points of intersection of their graphs, because points of intersection satisfy both equations simultaneously.

8.EE.C.8b Solve systems of two linear equations in two variables using the substitution method and estimate solutions by graphing the equations. Solve simple cases by inspection. For example: by inspection, conclude that 3x+2y=5 and 3x+2y=6 have no solution because 3x+2y cannot simultaneously be 5 and 6. Solve 3x+y=30 and y=2x using the substitution method;

8.F.A.1: Understand that a function is a rule that assigns to each input exactly one output. The graph of a function is the set of ordered pairs consisting of an input and the corresponding output.

8.F.A.2: Compare properties (e.g. rate of change, intercepts, domain and range) of two functions each represented in a different way (algebraically, graphically, numerically in tables, or by verbal descriptions).

8.F.B.5: Describe qualitatively the functional relationship between two quantities by analyzing a graph (e.g. where the function is increasing or decreasing, linear or nonlinear). Sketch a graph that exhibits the qualitative features of a function that has been described verbally.

Mathematical Practices

MP.1 Make sense of problems and persevere in solving them

MP. 2 Reason abstractly and quantitatively

MP.3 Construct viable arguments and critique the reasoning of others

MP. 4 Model with mathematics

MP. 5 Use appropriate tools strategically

MP. 6 Attend to precision

MP. 7 Look for and make use of structure

MP. 8 Look for and express regularity in repeated reasoning

| Career Readiness, Life Literacies and Key Skins | | | | |
|---|---|---|--|--|
| Standard Performance Expectations | | Core Ideas | | |
| 9.4.12.CI.1 | Demonstrate the ability to reflect, analyze, and use creative skills and ideas (e.g., 1.1.12 prof.CR3a). | With a growth mindset, failure is an important part of success. | | |
| 9.4.12.CT.1 | Identify problem-solving strategies used in the development of an innovative product or practice (e.g., 1.1.12acc.C1b, 2.2.12.PF.3). | Collaboration with individuals with diverse experiences can aid in the problem-solving process, particularly for global issues where | | |
| 9.4.12.CT.2 | Explain the potential benefits of collaborating to enhance critical thinking and problem solving (e.g., 1.3E.12profCR3.a). | | | |

areer Readiness, Life Literacies and Key Skills

| | | | | diverse solutions are needed. | |
|--|-------------------------|--|---|--|--|
| 9.4.12.TL.1 Assess digital tools ba | | ased on features such | | Digital tools differ in features, | |
| as accessibility option | | | cities, and | capacities, and styles. Knowledge | |
| | utility for accomplish | | ecific task | of different digital tools is helpful | |
| (e.g., W.11-12.6.). | | | | in selecting the best tool for a | |
| | ~ | | | given task. | |
| 9.4.8.TL.3 | Select appropriate too | ols to or | ganize and | Some digital tools are appropriate | |
| | present information d | 1g1tally. | | for gathering, organizing, | |
| | | | | analyzing, and presenting | |
| | | | | information, while other types of | |
| | | | | digital tools are appropriate for | |
| | | | | creating text, visualizations, | |
| | | | | models, and communicating with | |
| Control Ideo/Enduring Une | lorstanding: | Esson | tial/Guiding Our | otion: | |
| Chanter 3 | derstanding. | Chant | ter 3. Why are | granhs helnful? | |
| Lessons 1-3. A linear rela | ationshin has a | 1 | How can you | use a table to determine if there is a | |
| constant rate of change. It | n a proportional | 1. | proportional re | elationship between two | |
| linear relationship betwee | en two quantities a | | quantities? | | |
| and b: the ration b/a is co | nstant, the change in | 2. In any linear relationship, why is the slope always | | | |
| b / change in a is constant, and the graph | | | the same? | | |
| passes through the origin. The slope of a line | | | 3. What is the relationship among the unit rate, slope, | | |
| is the ratio of the vertical change (rise) | | | and constant r | ate of change of a proportional linear | |
| between any two points on a line and the | | | relationship? | | |
| horizontal change (run) between the same two | | | How does the | y-intercept appear in these three | |
| points. The slope formula can be used to find | | | representation | s: table, equation, and graph? | |
| the slope of the line betwee | een any two points on | 5. | How can the x | -intercept and y-intercept be used to | |
| the line. A linear equation | that describes a | | graph a linear | equation? | |
| constant rate of change is | called direct | 6. | How does usin | ng the point-slope form of a linear | |
| variation, In a direct varia | ation relationship, the | | equation make | e it easier to write the equation of a | |
| ratio of t/x is a constant k. The variable y is | | | line? | | |
| said to vary directly with x. This relationship | | | How can you | use a graph to solve a system of | |
| can be represented as $y/x = k$ or $y = kx$. | | | equations? | a live a sustain of a sustion of | |
| Lessons 4-6: The slope-intercept form of a | | 8. | How can you | solve a system of equations? | |
| slope and h is the v-intercent. To grade an | | Chant | tor 1. How can | wa madal relationshins between | |
| equation in slope intercent form using the | | Guant | ities? | we model relationships between | |
| slope and v-intercent ¹) graph the v-intercent | | quant 1 | How can you | use a graph to write an equation? | |
| 2) from the v-intercept use the slope to find the | | 2 | How do tables | and graphs represent relations? | |
| next point. 3) draw a line passing through both | | 3. | How does the | domain affect the range in a | |
| points. To graph functions using the x- and | | | function? | | |
| v-intercepts: 1) Find the x-intercept by | | | | | |

| replacing y with 0 and solving for x, 2) find the y-intercept by replacing x with 0 and solving for y, 3) Locate the two intercepts on a coordinate plane and draw a line passing through both points. Lessons 7-8 : A system of equations is a collection of two or more equations with the | 4. How can functions be used to solve real-world situations? 5. What are the advantages and disadvantages to representing a function as an equation instead of a graph? 6. How is the initial value of a function represented in a table and in a graph? |
|---|--|
| same variables. A system of equations can | 7. How can you use a table or a graph to determine if |
| have the following: 1) one solution - lines intersect at a point 2) no solution- parallel | a function is linear or nonlinear? 8 When does the graph of a guadratic function open |
| lines, or 3) infinitely many solutions - same | upward or downward? |
| line. A system can also be solved algebraically | 9. What are some advantages of displaying the |
| using substitution. | relationship between two quantities using a qualitative graph? |
| Chapter 4 | |
| Lessons 1-2: A relation is a set of ordered | |
| pairs that can be represented as a table or a | |
| graph. | |
| Lessons 3-6: A function is a special type of | |
| relation in which each member of the domain | |
| is parted with exactly one member in the | |
| Lesson 7-9: Some functions are linear and | |
| others are nonlinear. You can use a table or a | |
| graph to make the determination. If a function | |
| is linear, its graph is a straight line and a table | |
| of values for the function exhibits a constant | |
| rate of change. A nonlinear function is a | |
| function whose graph is not a straight line and | |
| a table of values for the function displays a | |
| rate of change that is not constant. | |
| Content: | Skills(Objectives): |
| Chapter 3: | Chapter 3: |
| 3.1: Constant Rate of Change | 3.1: Identify proportional and nonproportional linear |
| 3.2: Slope | relationships by finding a constant rate of change. |
| 3.3: Equations in y=mx Form | 3.2: Use tables and graphs to find the slope of a line. |
| 3.4: Slope-Intercept Form | 3.3: Use direct variation to solve problems. |
| 3.5: Graph a Line Using Intercepts | 3.4: Graph linear equations using the slope and |
| 3.6: Write Linear Equations | y-intercept. |
| 3.7: Solve Systems of Equations by Graphing | 3.5: Graph an equation using the x- and y-intercepts. |
| 3.8: Solve Systems of Equations Algebraically | 3.6: Write an equation of a line. |
| | 3.7: Solve systems of linear equations by graphing. |
| Chapter 4: | 3.8: Solve systems of equations algebraically. |
| 4.1: Represent Relationships | |
| 4.2: Relations | |

| 4.3: Functions | Chapter 4: | |
|---|--|--|
| 4.4: Linear Functions | 4.1: Translate tables and graphs into linear equations. | |
| 4.5: Compare Properties of Functions | 4.2: Represent relations using tables and graphs. | |
| 4.6: Construct Functions | 4.3: Find function values and complete function tables. | |
| 4.7: Linear and NonLinear Functions | 4.4: Represent linear functions using tables and graphs. | |
| 4.8: Quadratic Functions | 4.5: Compare properties of functions represented in | |
| 4.9: Qualitative Graphs | different ways. | |
| | 4.6: FInd and interpret the rate of change and initial value | |
| | of a function. | |
| | 4.7: Determine whether a function is linear or nonlinear. | |
| | 4.8: Graph quadratic functions. | |
| | 4.9: Sketch and describe qualitative graphs. | |
| Interdisciplinary Connections: | | |
| Interdisciplinary connections are integrated in each unit with connections to the mathematical practices. | | |
| Stage 2: Assessment Evidence | | |
| Performance Task(s): | Other Evidence: | |
| 8.EE.C.7: The Sign of Solutions | Online and Written Assignments | |
| 8.EE.C.7: Sammy's Chipmunk and Squirrel | Mid Chapter Quizzes | |
| Observations | End of Chapter Assessments | |
| 8.EE.B.5: Coffee by the Pound | End of Unit Common Assessments | |
| 8.EE.B.5: Who Has the Best Job? | | |
| 8.EE.B.5: Peaches and Plums | | |
| 8.EE.B.6: Slopes Between Points on a Line | | |
| 8.F.A.3: Introduction to Linear Functions | | |
| 8.F.B.4: Baseball Cards | | |
| 8.F.B.4: Video Streaming | | |
| 8.EE.C.8c: <u>Summer Swimming</u> | | |
| 8.EE.C.8: Cell Phone Plans | | |
| 8.EE.C.8: Kimi and Jordan | | |
| 8 FF C So: The Intersection of Two Lines | | |

8.F.A.1: <u>Function Rules</u>

8.F.A.1: Introducing Functions 8.F.A.2: Battery Charging

Stage 3: Learning Plan

| Learning Opportunities/Strategies: | Resources: | | |
|---|---|--|--|
| Use various Think-Pair-Share strategies | Glencoe Math Course 3 Textbook (Chapters 3-4) | | |
| provided by Glencoe for each lesson. | IXL | | |
| | Kahoot | | |
| Lesson 3.4: Have students work in pairs. Have | Khan Academy | | |
| them discuss one exercise with student 1 | Lesson Presentations | | |
| leading the discussion. After everyone agrees | Graphing Calculator | | |
| on the solution, each student individually | Google Forms and Sheets | | |
| records their answer. Repeat the process with | | | |

another exercise with student 2 leading the discussion. Continue rotating the leader role until all of the exercises have been completed. Lesson 3.5: Have students generate their own problem involving an equation expressed in standard form. Have students trade their problem with a partner, solve each other's problem and graph each other's equation, and discuss any differences in solutions. Lesson 3.6: Give them about two minutes of "think time." Then have them work with a partner to complete 2 exercises and discuss their responses. Then have them work individually to complete four more exercises. Upon completion, have them discuss their solutions with their partner and resolve any differences. Lesson 3.7: Have students work in small teams to complete one exercise, in pairs to complete exercise another exercise, and independently to complete a third exercise. Then have the original teams discuss their responses to the third exercise. Lesson 3.8: Have students work in pairs to compare and contrast solving a system of equations graphically and solving a system of equations algebraically. Then they should compile a list of pros and cons for each method. Lesson 4.1: Have students write a real-world problem and trade their partners with a partner. Each partner should create a table of values, create a graph, and write an equation that represents the relationship. Have students check each other's work, and discuss and resolve any differences. Lesson 4.2: Have students work in groups of

3-4 to label a copy of the coordinate plane with at least one error. Then have students trade papers with another group. Each group should find and correct the error(s).

Lesson 4.3: Have students create their own problem. Students trade their problems, solve each other's problems, and compare solutions

ALEKS Gimkit Google apps for education Desmos Woot Math Quizizz Quizalize Flocabulary Brain Pop Mash-Up Math Easel by Teachers Pay Teachers Classkick Edulastic

Math Literacy

- I can solve a word problem graphic organizer
- Think pair share graphic organizer
- Vocabulary <u>Word Map</u>
- Frayer Model
- Collection of Graphic Organizers

LGBT and Disabilities Resources:

- <u>LGBTQ-Inclusive Lesson & Resources by Garden</u> <u>State Equality and Make it Better for Youth</u>
- <u>LGBTQ+ Books</u>
- Inclusive Math Class

DEI Resources:

- Learning for Justice
- GLSEN Educator Resources
- <u>Supporting LGBTQIA Youth Resource List</u>
- <u>Respect Ability: Fighting Stigmas, Advancing</u> <u>Opportunities</u>
- <u>NJDOE Diversity, Equity & Inclusion Educational</u> <u>Resources</u>
- Diversity Calendar

| If the solutions do not agree students work together to find the errors. Lesson 4.4: For each exercise, have students create a different representation than the one given. Lesson 4.5: Assign students to 3 person teams. Each team completes 4 exercises with a different team member leading each exercise and making sure each team member understands the problem before moving on. Lesson 4.6: Have students work in pairs. Give them one minute to think through their responses to one exercise. Then have them share their responses with their partner and discuss any differences in their solutions. Have them repeat this process for 3 more exercises. Lesson 4.7: Students work to facts and one fib about linear functions or nonlinear functions. Students then form teams of 3. The job of the team is to identify the fib in each group of statements. Lesson 4.8: Have students work in pairs to complete the graphic organizer, and write a definition of quadratic function in their own words. Have them trade their definition with another pair and discuss any differences. | | |
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| | another pair and discuss any differences. | |

Differentiation *Please note: Teachers who have students with 504 plans that require curricular accommodations are to refer to Struggling and/or Special Needs Section for differentiation

| High-Achieving | On Grade Level | Struggling Students | Special Needs/ELL |
|-----------------------------|------------------------|-------------------------|---------------------------------------|
| Students | Students | | |
| Khan Academy | Tutoring | Provide a highly | Any student requiring further |
| Project based learning | Tables | structured, predictable | accommodations and/or modifications |
| Tablets | Graphic organizers | learning environment | will have them individually listed in |
| Challenging problems | Differentiation of | Provide | their 504 Plan or IEP. These might |
| with higher degree of | learning strategies: | organizers/study | include, but are not limited to: |
| difficulty | visual, auditory, | guides | breaking assignments into smaller |
| Higher order thinking | kinetic and | Lessons designed to | tasks, giving directions through |
| questions | cooperative | the style of learning | several channels (auditory, visual, |
| Differentiation of pacing | Technology | that matches the | kinesthetic, model), and/or small |
| and activities | connection | student | group instruction for reading/writing |
| Differentiation of learning | Practice Assignments | Cooperative Learning | |
| strategies: visual, | Puzzle time activities | Positive | ELL supports should include, but are |
| auditory, kinetic and | Record and practice | reinforcement | not limited to, the following:: |
| cooperative | journal | Announce test with | Extended time |
| Enrichment and extension | Differentiating the | adequate prep time | Provide visual aids |
| Technology connection | lesson activities | | Repeated directions |

| Practice assignments | Lesson tutorials | Lessons presentation | Differentiate based on proficiency |
|------------------------|------------------|----------------------|-------------------------------------|
| Puzzle time activities | Skills review | available on google | Provide word banks |
| Record and practice | handbook | classroom | Allow for translators, dictionaries |
| journal | | Frequent check for | |
| | | understanding | |
| | | Break down task into | |
| | | manageable units | |
| | | One-on-one | |
| | | instruction | |
| | | Tutoring | |
| | | Pair student with a | |
| | | high achieving | |
| | | student | |

<u>Unit Title</u>: Unit 4: Scatterplots, Inequalities, Financial Literacy

Stage 1: Desired Results

Standards & Indicators:

A.CED.A.1 - create equations and inequalities in one variable and use them to solve problems

A.CED.A.2 – create equations in two or more variables to represent relationships between quantities; graph equations on coordinate axes with labels and scales

A.CED.A.3 – represent constraints by equations or inequalities and by systems of equations and/or inequalities, interpret solutions as viable or nonviable options in a modeling context

A.REI.B.3 –solve linear equations and inequalities in one variable, including equations with coefficients represented by letters

A.REI.D.12 – graph the solutions to a linear inequality in two variables as a half plane and graph the solution set to a system of linear inequalities in two variables as the intersection of the corresponding half planes

8.SP.1 Construct and interpret scatter plot for bivariate measurement data to investigate patterns of association between two quantities. Describe patterns such as clustering, outliers, positive or negative association, linear association, and nonlinear association.

8.SP.2 Know that straight lines are widely used to model relationships between two quantitative variables. For scatter plots that suggest a linear association, informally fit a straight line, and informally assess the model fit by judging the closeness of the data points to the line.

8.SP.3 Use the equation of a linear model to solve problems in the context of bivariate data interpreting the slope and intercept. For example, in a linear model for a biology experiment, interpret a slope of 1.5 cm/hr as meaning that an additional hour of sunlight each day is associated with an additional 1.5 cm in mature

plant height.

8.SP.4 Understand the patterns of association can also be seen in bivariate categorical data by displaying the frequencies and relative frequencies in a two-way table. Construct and interpret a two-way table summarizing data on two categorical variables collected from the same subjects. Use relative frequencies calculated for rows or columns to describe possible association between the two variables. For example, collect data from students in your class on whether or not they have a curfew on school nights and whether or not they have assigned chores at home. Is there evidence that those who have a curfew also tend to have chores?

Integration of Climate Change:

8.SP.A.1 Construct and interpret scatter plots for bivariate measurement data to investigate patterns of association between two quantities. Describe patterns such as clustering, outliers, positive or negative association, linear association, and nonlinear association. Z
 Climate Change Example: Students may construct and interpret scatterplots of measurement data to investigate patterns of association in bivariate data involving the amount of a greenhouse gas in the

atmosphere and its effect on temperature.

8.SP.A.3 Use the equation of a linear model to solve problems in the context of bivariate measurement data, interpreting the slope and intercept. For example, in a linear model for a biology experiment, interpret a slope of 1.5 cm/hr as meaning that an additional hour of sunlight each day is associated with an additional 1.5 cm in mature plant height. Z
 Climate Change Example: Students may use the equation of a linear model to interpret the slope when

Climate Change Example: Students may use the equation of a linear model to interpret the slope when comparing local and global precipitation rates for rainfall in different regions.

- A.CED.A.1 Create equations and inequalities in one variable and use them to solve problems. Include equations arising from linear and quadratic functions, and simple rational and exponential functions. Climate Change Example: Students may create equations and/or inequalities to represent the economic impact of climate change.
- A.CED.A.3 Represent constraints by equations or inequalities, and by systems of equations and/or inequalities, and interpret solutions as viable or nonviable options in a modeling context. For example, represent inequalities describing nutritional and cost constraints on combinations of different foods. Z Climate Change Example: Students may represent constraints describing the economic impact of climate change by equations, inequalities, and/or by systems of inequalities, and interpret solutions as viable or nonviable options.

Mathematical Practices

MP.1 Make sense of problems and persevere in solving them

MP. 2 Reason abstractly and quantitatively

- MP.3 Construct viable arguments and critique the reasoning of others
- MP. 4 Model with mathematics
- MP. 5 Use appropriate tools strategically
- MP. 6 Attend to precision
- MP. 7 Look for and make use of structure
- MP. 8 Look for and express regularity in repeated reasoning

| Career Readiness, Life Literacies and Key Skills | | | | |
|--|--|--|--|--|
| Standard | Performance | Expectations | Core Ideas | |
| 9.1.8.PB.1 | Predict future expenses or opportunities that should be included in the budget planning process. | | A budget aligned with an individual's financial goals can help prepare for life events. | |
| 9.1.8.CP.3 | Explain the purpose c credit record, the fact credit scores. | of a credit score and ors and impact of | There are strategies to build and maintain a good credit history. | |
| 9.4.12.CI.1 | Demonstrate the ability to reflect, analyze, and use creative skills and ideas (e.g., 1.1.12 prof.CR3a). | | With a growth mindset, failure is an important part of success. | |
| 9.4.12.CT.1 | Identify problem-solving strategies used in the development of an innovative product or practice (e.g., 1.1.12acc.C1b, 2.2.12.PF.3). | | Collaboration with individuals with diverse experiences can aid in the problem-solving process, particularly for global issues where | |
| 9.4.12.CT.2 | Explain the potential benefits of collaborating to enhance critical thinking and problem solving (e.g., 1.3E.12profCR3.a). | | diverse solutions are needed. | |
| 9.4.12.TL.1 | Assess digital tools based on features such as accessibility options, capacities, and utility for accomplishing a specific task (e.g., W.11-12.6.). | | Digital tools differ in features, capacities, and styles. Knowledge of different digital tools is helpful in selecting the best tool for a given task. | |
| 9.4.8.TL.3 | Select appropriate too present information d | ols to organize and ligitally. | Some digital tools are appropriate for gathering, organizing, analyzing, and presenting information, while other types of digital tools are appropriate for creating text, visualizations, models, and communicating with others. | |
| Central Idea/Enduring Un | derstanding: | Essential/Guiding Que | estion: | |
| Glencoe Chapter 9: Lessons 1-3: A scatter plot is used to explore possible relationships between a data set with two variables. The data may have a positive, negative or no relationship. A line of best fit is | | Chapter 9: Why is learning mathematics important? 1. What are the inferences that can be drawn from sets of data points having a positive association and a negative association? 2. Why do we estimate a line of best fit for a scatter | | |
| a line that is very close to most of the data points. A two-way table shows data from one sample group as it relates to two different categories. | | plot? 3. How is a two-way table used when determining possible associations between two different categories from the same sample group? 4. What does the length of the "whiskers" in a box plot say about the data? | | |

Lessons 4-6: Data with one variable are called univariate data and can be described by a measure of center, such as mean, median, mode, or range. Quantitative data are data that can be measured. The data can be divided into four equal parts, called quartiles. The five-number summary provides a numerical way of characterizing a set of data. The mean absolute deviation of a set of data is the average distance between each data value and the mean. The standard deviation of a set of data is calculated value that shows how the data deviates from the mean of the data.

Algebra Chapter 5:

A linear inequality is an open sentence that contains \langle , \rangle, \leq , or \geq . Inequalities can be solved by using algebraic methods similar to solving equations. Inequalities involving absolute value can be solved by writing them as compound inequalities. Inequalities in two variables are solved by graphing the inequality as if it were an equation, and then shading the half-plane that makes the inequality true.

Financial Literacy:

To support the path towards postsecondary success, students require opportunities to understand and develop both career awareness and personal financial literacy. Standard 9.1 Personal Financial Literacy outlines the important fiscal knowledge, habits, and skills that must be mastered in order for students to make informed decisions about personal

- make informed decisions about personal finance. **Content: Skills(Objectives): Chapter 9: Chapter 9:** 9.1: Scatter Plots 9.1: Construct and make conjectures about scatter plots. 9.2: Lines of Best Fit 9.2: Draw lines of best fit and use them to make 9.3: Two-Way Tables predictions about data. 9.4: Descriptive Statistics 9.3: Construct and interpret two-way tables. 9.5: Measures of Variation 9.4: Find the measures of center and variation. 9.6: Analyze Data Distributions 9.5: Find and interpret the mean absolute deviation for a set of data.
 - 9.6: Analyze data distributions.

- 5. How does the mean absolute deviation describe the variation of a set of data?
- 6. Why is the median used to describe the center of non-symmetric distribution instead of the mean?

Algebra Chapter 5

- 1. How do you solve an inequality by using the different arithmetic operations?
- 2. How do you solve and graph a compound inequality?
- 3. How do you solve and graph an absolute value inequality?

Financial Literacy

- 1. How can we create and plan a budget based on income, education, etc?
- 2. What are strategies to build credit?
- 3. What is a credit score?

| Algebra I Text: Lesson 5.1 Solving Inequalities by | Inequalities: 1 Solve an inequality by using arithmetic operations |
|--|---|
| Addition/Subtraction | 2. Solve and graph a compound inequality. |
| Lesson 5.2 Solving Inequalities by | 3. Solve and graph an absolute value inequality |
| Multiplication/Division | 4. Graph a two variable inequality on a Cartesian |
| Lesson 5.3 Solving Multi Step Inequalities | plane |
| Lesson 5.4 Solving Compound Inequalities | - |
| Lesson 5.5 Solving Inequalities Involving | |
| Absolute Value | |
| Lesson 5.6 Graphing Inequalities in Two | |
| Variables | |
| Financial Literacy | |
| Occupation research | |
| Monthly Income & Budgeting | |
| Savings | |
| Interdisciplinary Connections: Interdisciplinary connections are integrated in ea | ch unit with connections to the mathematical practices. |
| Stage 2: As | sessment Evidence |
| Performance Task(s): | Other Evidence: |
| A-CED.A.1 Paying the rent | Online and Written Assignments |
| https://www.illustrativemathematics.org/conte | Mid Chapter Quizzes |
| nt-standards/HSA/CED/A/1/tasks/581 | End of Chapter Assessments |
| | End of Unit Common Assessments |
| A.CED.A.3 Dimes and Quarters | |
| https://www.illustrativemathematics.org/conte | |
| nt-standards/HSA/CED/A/3/tasks/220 | |
| A REL B 3 Reasoning with linear inequalities | |
| https://www.illustrativemathematics.org/conte | |
| nt_standards/HSA/REI/B/3/tasks/807 | |
| III-stanuarus/IISA/IKLI/D/J/asks/00/ | |
| A.REI.D.12 Fishing Adventures 3 | |
| https://www.illustrativemathematics.org/conte | |
| nt-standards/HSA/REI/D/12/tasks/644 | |
| | |
| F.IF.A.2 Yam in the Oven | |
| https://www.illustrativemathematics.org/conte | |
| nt-standards/HSF/IF/A/2/tasks/625 | |
| SIDC 7-9 Coffee and Crime | |
| https://www.illustrativemathematics.org/conte | |
| nt_standards/HSS/ID/B/6/tasks/1307 | |
| nt Sundards/1155/12/2/0/tasks/150/ | |

| Financial Literacy | | | | | |
|--|--|--|--|--|--|
| Math in real world | | | | | |
| Stage 3: Learning Plan | | | | | |
| Math in real world Learning Opportunities/Strategies: Lesson 9.1: Before constructing the scatter plot for an exercise, have students study the data in the table and make a conjecture about the association. Have them explain why their association makes sense in the real world context of the problem. Lesson 9.2: Have students work in pairs and write down two facts and one fib about scatter plots, associations, and lines of best fit. Call on individuals to read their facts and fib and have the class vote to decide which statement is the fib. Lesson 9.3: Have students work in pairs to complete two exercises. Have them trade their solutions with another pair of students and discuss any differences. Lesson 9.4: Have students work with a partner to explain the different meanings of the word mean. Lesson 9.5: Have students work in teams of three. Each team member is to pick one of the following topics to research: normal distribution, standard deviation, or variance. Students in the class working on the same topic get together to decide what is important and how to teach it to the rest of the team. Each expert returns to the team to teach the team members about their researched topic. Lesson 9.6: Have students work with a partner to complete the vocabulary start up. Have each student read the terms aloud and decide upon the best description, reading each description aloud. Call on one set of pairs to share their responses with the class. | : Learning Plan Resources: Glencoe Math Course 3 Textbook (Chapters 9) Glencoe Algebra I (Chapter 5) IXL Kahoot Khan Academy Lesson Presentations Graphing Calculator Google Forms and Sheets ALEKS Gimkit Google apps for education Desmos Woot Math Quizizz Quizalize Flocabulary Brain Pop Mash-Up Math Easel by Teachers Pay Teachers Classkick Edulastic Math Literacy I can solve a word problem graphic organizer Vocabulary Word Map Frayer Model Collection of Graphic Organizers LGBT and Disabilities Resources: LGBTQ+H Books Inclusive Math Class DEI Resources: Learning for Justice GL SEN Educator Resources | | | | |
| the best description, reading each description aloud. Call on one set of pairs to share their responses with the class. | <u>LOB IQ+ BOOKS</u> <u>Inclusive Math Class</u> DEI Resources: <u>Learning for Justice</u> <u>GLSEN Educator Resources</u> <u>Supporting LGBTQIA Youth Reso</u> <u>Respect Ability: Fighting Stigmas, Opportunities</u> NIDOE Diversity Equity & Inclus | | | | |
| | <u>NJDOE Diversity, Equity & Inclusion Educational</u> <u>Resources</u> | | | | |

| | | • <u>Diversity Cale</u> | endar | | |
|---|--------------------------|-------------------------|---------------------------------------|--|--|
| Differentiation *Please note: Teachers who have students with 504 plans that require curricular | | | | | |
| accommodations are to re | efer to Struggling and/o | r Special Needs Section | n for differentiation | | |
| High-Achieving | On Grade Level | Struggling Students | Special Needs/ELL | | |
| Students | Students | D 1 1 11 | | | |
| Khan Academy | Tutoring | Provide a highly | Any student requiring further | | |
| Project based learning | Tables | structured, predictable | accommodations and/or modifications | | |
| Tablets | Graphic organizers | learning environment | will have them individually listed in | | |
| Challenging problems | Differentiation of | Provide | their 504 Plan or IEP. These might | | |
| with higher degree of | learning strategies: | organizers/study | include, but are not limited to: | | |
| difficulty | visual, auditory, | guides | breaking assignments into smaller | | |
| Higher order thinking | kinetic and | Lessons designed to | tasks, giving directions through | | |
| questions | cooperative | the style of learning | several channels (auditory, visual, | | |
| Differentiation of pacing | Technology | that matches the | kinesthetic, model), and/or small | | |
| and activities | connection | student | group instruction for reading/writing | | |
| Differentiation of learning | Practice Assignments | Cooperative Learning | | | |
| strategies: visual, | Puzzle time activities | Positive | ELL supports should include, but are | | |
| auditory, kinetic and | Record and practice | reinforcement | not limited to, the following:: | | |
| cooperative | journal | Announce test with | Extended time | | |
| Enrichment and extension | Differentiating the | adequate prep time | Provide visual aids | | |
| Technology connection | lesson activities | Lessons presentation | Repeated directions | | |
| Practice assignments | Lesson tutorials | available on google | Differentiate based on proficiency | | |
| Puzzle time activities | Skills review | classroom | Provide word banks | | |
| Record and practice | handbook | Frequent check for | Allow for translators, dictionaries | | |
| journal | | understanding | | | |
| 5 | | Break down task into | | | |
| | | manageable units | | | |
| | | One-on-one | | | |
| | | instruction | | | |
| | | Tutoring | | | |
| | | Pair student with a | | | |
| | | high achieving | | | |
| | | student | | | |

Pacing Guide

| Course Name | Content/Resources | Standards |
|---------------------------------------|----------------------------------|------------------|
| UNIT 1: | | |
| Transformations/Geometric | CHAPTERS: | 8.G.1 |
| sequences/ Pythagorean Theorem | Glencoe Chapters 5-7 | 8.G.2 |
| (41 Days) | | 8.G.3 8.G.4 |
| | Unit Assessment: 1-2 days | 8.G.5 |
| | | |
| LINIT 2. | | |
| Contraction Distance Description | CHARTERS. | |
| Scatter Plots, volume, Real life | CHAPTERS: | 8.G.9 |
| (28 Days) | Giencoe Chapters 8 & 1 | 8.EE.1 8 FE 3 |
| (So Days) | Unit Online Assessment: 1.2 days | 8.NS.1 |
| | Omt Omme Assessment. 1-2 days | 8.NS.2 |
| UNIT 3: | · | · |
| Equations with One and Two | CHAPTERS: | 8.EE.C.7 |
| Variables & Functions | Glencoe Chapter 3- 4 | 8.EE.B.5: |
| (40 Days) | | 8.EE.B.6: |
| | Unit Online Assessment: 1-2 days | 8.F.A.2: |
| | | 8 F A 3 |
| | | 8.EE.C.8 |
| | | 8.F.A.1:. |
| | | 8.F.B.5: |
| UNIT 4: | | |
| Scatterplots, Inequalities, Financial | CHAPTERS: | A.CED.A.1 |
| Literacy | Glencoe Chapter 9 | A.CED.A.2 |
| (40 days) | Algebra Chapter 5 | A.CED.A.3 |
| | Financial Literacy | A.REI.5 |
| | | 8.SP.1 |
| | Unit Online Assessment: 1-2 days | 8.SP.2 |
| | | 8.SP.3 |
| | | 8.SP.4 |