Unit Title: Unit 1: Equations, Relations and Functions

Stage 1: Desired Results

Standards & Indicators:

A.CED.A.1 – create equations and inequalities in one variable and use them to solve problems

A.REI.D.11 – explain why the x-coordinates of the points where the graphs of two equations y = f(x) and y = g(x) intersect are the solutions of the equations f(x) = g(x). Find the solutions using technology, make tables of values and include cases where the functions are linear, polynomial, rational, absolute value, exponential and logarithmic functions.

F.IF.B.4 – for a function that models a relationship between two quantities, interpret key features of the graph and tables and sketch graphs given a verbal description of the relationship

F.IF.B.6 – calculate and interpret the average rate of change of a function over a specified interval, estimate rate of change from a graph

F.IF.C.7 – graph functions expressed symbolically and show key features of the graph using technology if necessary

F.IF.C.9 – compare properties of two functions each represented in a different way (algebraically or graphically)

Career Readiness, Life Literacies and Key Skills			
Standard	Performance	Expectations	Core Ideas
9.4.12.CI.1	Demonstrate the ability use creative skills and i (e.g.1.1.12prof.CR3a).	to reflect, analyze, and deas	With a growth mindset, failure is an important part of success.
9.4.12.GCA.1	Collaborate with individ variety of potential solur effects and determine v (e.g., political. economic better than others (e.g., HS-ETS1-1, HS-ETS1-6.3.12.GeoGl.1, 7.1.IH.	tions to climate change why some solutions c, cultural) may work , SL.11-12.1., 2, HS-ETS1-4, IPERS.6,	Solutions to the problems faced by a global society require the contribution of individuals with different points of view and experiences.
9.4.12.CT.1	Identify problem-solving development of an inno practice (e.g., 1.1.12ac	vative product or	Collaboration with individuals with diverse experiences can aid in the problem-solving process, particularly for global issues where diverse solutions are needed.
Central Idea/Enduring Understanding:		Essential/Guiding Que	estion:
Chapter 1 Equations are mathematical sentences that state a relationship between two or more mathematical expressions. Solutions for equations can be found by isolating the variable on one side of the equal		At the end of the Unit, s Essential Questions:	tudents should be able to answer the

sign using the Properties of Equality. A system of equations consists of two or more equations with the same variables. Systems of equations can be solved by graphing or algebraically by using the elimination method, the substitution method, or with the use of matrices. Systems of inequalities can be solved by graphing.

Chapter 1- How are symbols useful in mathematics? How can you find the solution to a math problem?

Chapter 2- How can mathematical ideas be represented?

Chapter 2

Linear relations and functions have straight line graphs. The rate of change of a linear function is known as the slope and can be found using any two points on the line. The equation of a line can be written whenever two points or a point and the slope of the line are known. A line of fit can be used to approximate the relation between domain and range values of a data set that exhibits a linear trend.

Skills(Objectives):

Translate verbal expressions into algebraic expressions and equations and vice versa

Solve equations using the properties of equality

Solve one step and multi step inequalities

Find the rate of change

Determine the slope of a line

Solve systems of linear equations graphically and algebraically

Determine whether functions are one to one and/or onto

Determine whether functions are discrete or continuous

Identify linear and nonlinear functions by examining equations or graphs

Determine whether graphs of functions have line or point symmetry

Identify end behavior of graphs

Identify extrema of functions

Use the key features of functions to sketch graphs of linear and non linear functions

Graph and analyze piecewise defined functions

Content:

- 1.1 solving linear equations
- 1.2 solving linear inequalities
- 1.3 rate of change and slope
- 1.6 solving systems of equations
- 2.1 functions and continuity
- 2.2 linearity and symmetry
- 2.3 extrema and end behavior
- 2.4 sketching graphs of functions
- 2.5 graphing special functions
- 2.6 transformations of functions
- 2.7 solving equations by graphing

Graph and analyze step and absolute value functions

Identify the effects on graphs of functions by replacing f(x) with f(x) + k and f(x-h) for positive and negative values

Identify the effects on graphs of functions by replacing f(x) with af(x), f(ax)-af(x) and f(-ax)

Find x and y intercepts

Solve equations by examining graphs of the related functions

Interdisciplinary Connections:

Interdisciplinary connections are integrated in each unit with connections to the mathematical practices.

- 1. Make sense of problems and persevere in solving them
- 2. Reason abstractly and quantitatively
- 3. Construct viable arguments and critique the reasoning of others
- 4. Model with mathematics
- 5. Use appropriate tools strategically
- 6. Attend to precision
- 7. Look for and make use of structure
- 8. Look for and express regularity in repeated reasoning

Stage 2: Assessment Evidence

Performance Task(s):

A.REI.D.11 Ideal Gas Law

https://www.illustrativemathematics.org/content-standards/HSA/REI/D/11/tasks/1925

A.CED. 1 Paying the Rent

http://tasks.illustrativemathematics.org/content-standards/HSA/CED/A/1/tasks/581

F.IF.C.7c Graphs of Power Functions

https://www.illustrativemathematics.org/content-standards/HSF/IF/C/7/tasks/627

F.IF.C.7e Logistic Growth Model

https://www.illustrativemathematics.org/content-standards/HSF/IF/B/4/tasks/804

F.IF.C.9 Throwing Baseballs

https://www.illustrativemathematics.org/content-standards/HSF/IF/C/9/tasks/1279

Other Evidence:

Written and Online Assignments Exit Cards Mid Chapter Quizzes End of Chapter Assessments

Stage 3: Learning Plan

Learning Opportunities/Strategies:

Resources:

Glencoe Algebra 2 Textbook (Chapters 1 and 2)

Lesson 1.1 solving linear equations
Translate verbal phrases, identify number
properties, solve one step/multi step equations,
use properties of equality

Lesson 1.2 solving linear inequalities Solve one step/multi step inequalities, write an inequality, apply inequalities to real world situations

Lesson 1.3 rate of change and slope Find slope using coordinates, find slope using a graph

Interpret rate of change from real world problems

Lesson 1.6 solving systems of equations Solve a system of equations by: using a table, graphing, substitution method or elimination method

Lesson 2.1 functions and continuity
Find domain and range, graph a relation, evaluate
a function, identify discrete and continuous
functions

Lesson 2.2 linearity and symmetry Identify linear functions from equations and graphs, identify line and point symmetry

Lesson 2.3 extrema and end behavior
Describe the end behavior of linear and non-linear
functions, estimate the zeros ad extrema of a
graph, find end behavior and extrema
Lesson 2.4 sketching graphs of functions
Sketch a linear and non-linear graph, sketch a real
world function

Lesson 2.5 graphing special functions Graph and write a piece wise defined function, use a step function to model a real world problem, graph an absolute value function and identify the domain and range

Lesson 2.6 transformations of functions Describe and graph a translation of a function, describe and graph a reflection, describe and graph dilations, identify transformations IXL

Delta math

Edulastic

Kahoot

Classkick

NJSLA Digital Library

Khan Academy

Lesson Presentations and Videos

Graphing Calculator

Desmos

Google Apps for Education

LGBT and Disabilities Resources:

- LGBTQ-Inclusive Lesson & Resources by Garden
 State Equality and Make it Better for Youth
- LGBTQ+ Books

DEI Resources:

- <u>Learning for Justice</u>
- GLSEN Educator Resources
- Supporting LGBTQIA Youth Resource List
- Respect Ability: Fighting Stigmas, Advancing Opportunities
- NJDOE Diversity, Equity & Inclusion Educational Resources
- Diversity Calendar

Lesson 2.7 solving equations by graphing Find x and y intercepts of graphs, find the zeros of a function, solve an equation by graphing

Differentiation

*Please note: Teachers who have students with 504 plans that require curricular accommodations are to refer to Struggling and/or Special Needs Section for differentiation

Struggling and/or Special Needs Section for differentiation			
High-Achieving	On Grade Level	Struggling Students	Special Needs/ELL
Students	Students		
Khan Academy	Tutoring	Provide a highly	Any student requiring further
Project based learning	Tables	structured, predictable	accommodations and/or modifications
Tablets	Graphic organizers	learning environment	will have them individually listed in
Challenging problems	Differentiation of	Provide	their 504 Plan or IEP. These might
with higher degree of	learning strategies:	organizers/study	include, but are not limited to:
difficulty	visual, auditory,	guides	breaking assignments into smaller
Higher order thinking	kinetic and	Lessons designed to	tasks, giving directions through
questions	cooperative	the style of learning	several channels (auditory, visual,
Differentiation of pacing	Technology	that matches the	kinesthetic, model), and/or small
and activities	connection	student	group instruction for reading/writing
Differentiation of learning	Practice Assignments	Cooperative Learning	
strategies: visual,	Puzzle time activities	Positive reinforcement	ELL supports should include, but are
auditory, kinetic and	Record and practice	Announce test with	not limited to, the following::
cooperative	journal	adequate prep time	Extended time
Enrichment and extension	Differentiating the	Lessons presentation	Provide visual aids
Technology connection	lesson activities	available on google	Repeated directions
Practice assignments	Lesson tutorials	classroom	Differentiate based on proficiency
Puzzle time activities	Skills review	Frequent check for	Provide word banks
Record and practice	handbook	understanding	Allow for translators, dictionaries
journal		Break down task into	
		manageable units	
		One-on-one	
		instruction	
		Tutoring	
		Pair student with a	
		high achieving	
		student	

Unit Title: Unit 2: Quadratic and Polynomial Functions

Stage 1: Desired Results

Standards & Indicators:

A.CED.A.1 - create equations and inequalities in one variable and use them to solve problems

A.REI.D.11 explain why the x-coordinates of the points where the graphs of two equations y = f(x) and y = g(x) intersect are the solutions of the equations f(x) = g(x). Find the solutions using technology, make tables of values and include cases where the functions are linear, polynomial, rational, absolute value, exponential and logarithmic functions.

A.REI.D.12 – graph the solutions to a linear inequality in two variables as a half plane and graph the solution set to a system of linear inequalities in two variables as the intersection of the corresponding half planes

A.APR.B.2

Know and apply the Remainder Theorem: For a polynomial p(x) and a number a, the remainder on division by x - a is p(a), so p(a) = 0 if and only if (x - a) is a factor of p(x).

A.APR.B.3

solve linear equations and inequalities in one variable, including equations with coefficients represented by letters

A.APR.D.6

Rewrite simple rational expressions in different forms; write a(x)/b(x) in the form q(x) + r(x)/b(x), where a(x), b(x), q(x), and r(x) are polynomials with the degree of r(x) less than the degree of r(x), using inspection, long division, or, for the more complicated examples, a computer algebra system.

A.SSE.A.2

use the structure of an expression to identify ways to rewrite it

F.IF.B.4

for a function that models a relationship between two quantities, interpret key features of the graph and tables and sketch graphs given a verbal description of the relationship

F.IF.B.6

calculate and interpret interval, the average rate of change of a function over a specified interval, estimate rate of change from a graph

F.IF.C.8

write a function defined by an expression in different but equivalent forms to reveal and explain different properties of the function

F.IF.C.9

compare properties of two functions each represented in a different way (algebraically or graphically)

N.Q.A.2

define appropriate quantities for descriptive modeling

Career Readiness, Life Literacies and Key Skills			
Standard	Performance Expectations	Core Ideas	
9.4.12.CI.1	Demonstrate the ability to reflect, analyze, and use creative skills and ideas (e.g., 1.1.12prof.CR3a).	With a growth mindset, failure is an important part of success.	
9.4.12.CT.1	Identify problem-solving strategies used in the development of an innovative product or practice (e.g., 1.1.12acc.C1b, 2.2.12.PF.3).	Collaboration with individuals with diverse experiences can aid in the problem-solving process, particularly for global issues where diverse solutions are needed.	
9.4.12.GCA.1	Collaborate with individuals to analyze a variety of potential solutions to climate change effects and determine why some solutions (e.g., political. economic, cultural) may work better than others (e.g., SL.11-12.1., HS-ETS1-1, HS-ETS1-2, HS-ETS1-4, 6.3.12.GeoGl.1, 7.1.IH.IPERS.6, 7.1.IL.IPERS.7, 8.2.12.ETW.3).	Solutions to the problems faced by a global society require the contribution of individuals with different points of view and experiences.	

Central Idea/Enduring Understanding:

Chapter 3

The graphs of quadratic functions are called parabolas. Each parabola has a vertex, axis of symmetry, and a y-intercept. Quadratic equations can be solved by graphing, factoring, completing the square, and by using the quadratic formula. Transformations to the parent graph can be more readily identified if the quadratic equation is written in vertex form.

Chapter 4

An expression made up of a sum of monomials that contain one variable is called a polynomial in one variable. Pascal's Triangle is an easy way to find the coefficients of the expansion of the powers of binomials. Tables of values can be used to explore graphs of polynomial functions. Factoring, synthetic substitution, and Descartes' Rule of Signs can be used to solve equations or find the zeros of polynomial functions.

Essential/Guiding Question:

At the end of the Unit, students should be able to answer the Essential Questions:

Chapter 3 – Why do we use different methods to solve math problems?

Chapter 4 – Why is math used to model real-world situations?

Content:

- 3.1 graphing quadratic functions
- 3.2 solving quadratic equations by graphing
- 3.3 complex numbers
- 3.4 solving quadratic equations by factoring
- 3.5 solving quadratic equations by completing the square
- 3.6 the quadratic formula and the discriminant
- 3.7 quadratic inequalities

Skills(Objectives):

Graph quadratic functions

Find and interpret the maximum and minimum values of a quadratic functions

Solve quadratic functions by graphing

Estimate solutions of quadratic equations by graphing

- 4.3 dividing polynomials
- 4.4 graphing polynomial functions
- 4.5 analyzing graphs of polynomial functions
- 4.6 solving polynomial equations
- 4.7 proving polynomial identities
- 4.8 the remainder and factor theorem
- 4.9 roots and zeros

Perform operations with pure imaginary and complex numbers

Write quadratic equations in standard form

Solve quadratic equations by factoring

Solve quadratic equations by using the square root property

Solve quadratic equations by completing the square

Solve quadratic equations by using the quadratic formula

Use the discriminant to determine the number and type of roots of a quadratic equation

Graph quadratic inequalities in two variables

Solve quadratic inequalities in one variable

Divide polynomials using long division and synthetic division

Evaluate polynomial functions

Identify general shapes of graphs of polynomial functions

Graph polynomial functions and locate their zeros

Find the relative maxima and minima of polynomial functions

Factor polynomials

Solve polynomial equations by factoring

Prove polynomial identities

Prove polynomial identities and use them to describe numerical relationships

Evaluate functions by using synthetic substitution

Determine whether a binomial is a factor of a polynomial by using synthetic substitution

Determine the number and type of roots for a polynomial equation

Find the zeros of a polynomial function

Interdisciplinary Connections:

Interdisciplinary connections are integrated in each unit with connections to the mathematical practices.

1. Make sense of problems and persevere in solving them

- 2. Reason abstractly and quantitatively
- 3. Construct viable arguments and critique the reasoning of others
- 4. Model with mathematics
- 5. Use appropriate tools strategically
- 6. Attend to precision
- 7. Look for and make use of structure
- 8. Look for and express regularity in repeated reasoning

Stage 2: Assessment Evidence

Performance Task(s):

A.APR.B.2

The Missing Coefficient

https://www.illustrativemathematics.org/content-standards/HSA/APR/B/2/tasks/592

A.APR.B.3

Graphing from Factors III

https://www.illustrativemathematics.org/content-standards/HSA/APR/B/3/tasks/1657

A.APR.D.6

Combined Fuel Efficiency

https://www.illustrativemathematics.org/content-standards/HSA/APR/D/6/tasks/825

A.REI.D.12- Solution Sets

http://tasks.illustrativemathematics.org/content-standards/HSA/REI/D/12/tasks/1205

Other Evidence:

Written and Online Assignments

Exit Cards

Mid Chapter Quizzes

End of Chapter Assessments

End of Unit Common Assessments

Stage 3: Learning Plan

Learning Opportunities/Strategies:

Lesson 3.1 – graphing quadratic functions Graph a quadratic function by using a table, find the y-intercept, the axis of symmetry and x coordinate of the vertex, identify maximum and minimum values, apply quadratic equations to real world problems

Lesson 3.2 – solving quadratic equations by graphing

solve a quadratic equation and identify the number of real solutions (0,1,2), estimate the roots of a quadratic, solve a quadratic using a table and calculator

Lesson 3.3 - complex numbers

find the square root of negative numbers, find the products of imaginary numbers, solve in equation

Resources:

Glencoe Algebra 2 Textbook (Chapters 3 and 4)

IXL

Delta math

Edulastic

Kahoot

Classkick

NJSLA Digital Library

Khan Academy

Lesson Presentations and Videos

Graphing Calculator

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Google Apps for Education

LGBT and Disabilities Resources:

LGBTQ-Inclusive Lesson & Resources by Garden State Equality and Make it Better for Youth

with imaginary solutions, add, subtract, multiply and divide complex numbers

Lesson 3.4 – solving quadratic equations by factoring

translate sentences into equations, factor the GCF, solve equations using perfect squares and differences of squares, factor trinomials, solve equations by factoring

Lesson 3.5 – solving quadratic equations by completing the square solve an equation with rational and irrational roots, complete the square, solve an equation by completing the square, solve equations with imaginary solutions

Lesson 3.6 – the quadratic formula and the discriminant

solve a quadratic equation using the quadratic formula that contains: two rational roots, one rational root, irrational roots or complex roots, describe roots

Lesson 3.7 – quadratic inequalities Graph a quadratic inequality, solve a quadratic inequality graphically and algebraically, solve a real world problem using quadratic inequalities

Lesson 4.3 – dividing polynomials Divide a polynomial by a monomial, use long division to divide a trinomial by a binomial, use synthetic division to divide polynomials

Lesson 4.4 – graphing polynomial functions identify the degree and leading coefficient of polynomials, evaluate a polynomial function, find function values of variables

Lesson 4.5 – analyzing graphs of polynomial functions

Locate the zeros of a function, find the maximum and minimum points of a function, graph a polynomial model

Lesson 4.6 – solving polynomial equations factor using the sum and differences of cubes, factor by grouping, solve polynomial functions by factoring, write expressions and solve equations in quadratic form

Lesson 4.7 – proving polynomial identities

LGBTQ+ Books

DEI Resources:

- Learning for Justice
- GLSEN Educator Resources
- Supporting LGBTQIA Youth Resource List
- Respect Ability: Fighting Stigmas, Advancing Opportunities
- NJDOE Diversity, Equity & Inclusion Educational Resources
- <u>Diversity Calendar</u>

prove polynomial identities by writing proofs, use technology to prove that polynomials are identities

Lesson 4.8 – the remainder and factor theorem use synthetic substitution to evaluate functions, find function values, use the factor theorem

Lesson 4.9 – roots and zeros determine the number and type of roots of a function, find the number of positive, negative and imaginary zeros, use synthetic substitution to find zeros, use zeros to write a polynomial function

Differentiation

*Please note: Teachers who have students with 504 plans that require curricular accommodations are to refer to Struggling and/or Special Needs Section for differentiation

High-Achieving	On Grade Level	Struggling Students	Special Needs/ELL
Students	Students		
Khan Academy Project based learning Tablets Challenging problems with higher degree of difficulty Higher order thinking questions Differentiation of pacing and activities Differentiation of learning strategies: visual, auditory, kinetic and cooperative Enrichment and extension Technology connection Practice assignments Puzzle time activities Record and practice journal	Tutoring Tables Graphic organizers Differentiation of learning strategies: visual, auditory, kinetic and cooperative Technology connection Practice Assignments Puzzle time activities Record and practice journal Differentiating the lesson activities Lesson tutorials Skills review handbook	Provide a highly structured, predictable learning environment Provide organizers/study guides Lessons designed to the style of learning that matches the student Cooperative Learning Positive reinforcement Announce test with adequate prep time Lessons presentation available on google classroom Frequent check for understanding Break down task into manageable units One-on-one instruction Tutoring Pair student with a high achieving student	Any student requiring further accommodations and/or modifications will have them individually listed in their 504 Plan or IEP. These might include, but are not limited to: breaking assignments into smaller tasks, giving directions through several channels (auditory, visual, kinesthetic, model), and/or small group instruction for reading/writing ELL supports should include, but are not limited to, the following:: Extended time Provide visual aids Repeated directions Differentiate based on proficiency Provide word banks Allow for translators, dictionaries

Unit Title: Unit 3: Radical, Exponential and Logarithmic Functions

Stage 1: Desired Results

Standards & Indicators:

A.REI.A.2

Solve simple rational and radical equations in one variable, and give examples showing how extraneous solutions may arise.

A.REI.D.11

explain why the x-coordinates of the points where the graphs of two equations y = f(x) and y = g(x) intersect are the solutions of the equations f(x) = g(x). Find the solutions using technology, make tables of values and include cases where the functions are linear, polynomial, rational, absolute value, exponential and logarithmic functions.

A.SSE.A.2

use the structure of an expression to identify ways to rewrite it

A.SSE.B.4

Derive and/or explain the formula for the sum of a finite geometric series (when the common ratio is not 1), and use the formula to solve problems. For example, calculate mortgage payments

F.BF.A.1

determine an explicit expression, a recursive process or steps for calculation from a context

FIFR 4

for a function that models a relationship between two quantities, interpret key features of the graph and tables and sketch graphs given a verbal description of the relationship

F.IF.C.7

graph functions expressed symbolically and show key features of the graph using technology if necessary

F.IF.C.8

write a function defined by an expression in different but equivalent forms to reveal and explain different properties of the function

F.IF.C.9

compare properties of two functions each represented in a different way (algebraically or graphically)

F.LE.A.4

Understand the inverse relationship between exponents and logarithms. For exponential models, express as a logarithm the solution to abct = d where a, c, and d are numbers and the base b is 2, 10, or e; evaluate the logarithm using technology.

Career Readiness, Life Literacies and Key Skills			
Standard	Performance Expectations	Core Ideas	
9.4.12.Cl.1	Demonstrate the ability to reflect, analyze, and use creative skills and ideas (e.g., 1.1.12prof.CR3a).	With a growth mindset, failure is an important part of success.	
9.4.12.CT.1	Identify problem-solving strategies used in the development of an innovative product or practice (e.g., 1.1.12acc.C1b, 2.2.12.PF.3).	Collaboration with individuals with diverse experiences can aid in the problem-solving process, particularly	

		for global issues where diverse
		solutions are needed.
9.4.12.GCA.1	Collaborate with individuals to analyze a	Solutions to the problems faced by a
	variety of potential solutions to climate change	global society require the contribution
	effects and determine why some solutions	of individuals with different points of
	(e.g., political. economic, cultural) may work	view and experiences.
	better than others (e.g., SL.11-12.1.,	
	HS-ETS1-1, HS-ETS1-2, HS-ETS1-4,	
	6.3.12.GeoGl.1, 7.1.IH.IPERS.6,	
	7.1.IL.IPERS.7, 8.2.12.ETW.3).	

Central Idea/Enduring Understanding:

Chapter 5

The inverse of a function can be found by exchanging the domain and range of the function. Functions with a variable under a radical symbol are called radical functions. Two types of radical functions are square root functions and cube root functions. When solving radical equations, first isolate the radical, then raise each side to the power equal to the index of the radical, and finally, solve the resulting equation.

Chapter 6

An exponential equation is in the form y = bx, where b > 0 and $b \ne 1$. The equation represents exponential growth when b > 1 and exponential decay when 0 < b < 1. The inverse of an exponential function is the logarithmic function.

Essential/Guiding Question:

At the end of the Unit, students should be able to answer the Essential Questions:

Chapter 5 - How can you choose a model to represent a set of data?

Chapter 6 - How can you make good decisions? What factors can affect good decision making?

Content:

- 5.1 operations with functions
- 5.2 composition of functions
- 5.3 inverse functions and relations
- 5.4 graphing square root functions
- 5.5 graphing cube root functions
- 5.6 solving radical equations
- 6.1 graphing exponential functions
- 6.2 solving exponential functions and inequalities
- 6.3 geometric sequences and series
- 6.4 logarithms and logarithmic functions
- 6.6 properties of logarithms
- 6.7 common logarithms
- 6.8 natural logarithms
- 6.9 solving logarithmic equations and inequalities
- 6.10 using logarithms to solve exponential problems

Skills(Objectives):

Perform arithmetic operations with functions

Apply arithmetic operations with functions

Perform compositions of functions

Apply compositions of functions

Find the inverse of a function or relation

Determine whether two functions or relations are inverses

graph and analyze square root functions

graph and analyze cube root functions

solve equations containing radicals

solve inequalities containing radicals

graph exponential growth and decay functions

solve exponential equations and inequalities

use geometric sequences

find sums of geometric series

evaluate logarithmic expressions

graph logarithmic functions

simplify and evaluate expressions using the properties of logarithms

solve logarithmic equations using the properties of logarithms

solve exponential equations and inequalities using common logarithms

evaluate logarithmic expressions using the change of base formula

evaluate expressions involving the natural base and natural logarithm

solve exponential equations and inequalities using natural logarithms

solve logarithmic equations and inequalities

use logarithms to solve problems involving exponential growth and decay

use logarithms to solve problems involving logistic growth

Interdisciplinary Connections:

Interdisciplinary connections are integrated in each unit with connections to the mathematical practices.

- 1. Make sense of problems and persevere in solving them
- 2. Reason abstractly and quantitatively
- 3. Construct viable arguments and critique the reasoning of others
- 4. Model with mathematics
- 5. Use appropriate tools strategically
- 6. Attend to precision
- 7. Look for and make use of structure
- 8. Look for and express regularity in repeated reasoning

Performance Task(s): A.SSE.A.2 A Cubic Identity Stage 2: Assessment Evidence Other Evidence: Written and Online Assignments Exit Cards

https://www.illustrativemathematics.org/content-standards/HSA/SSE/A/2/tasks/919

A.SSE.B.4

Course of Antibiotics

https://www.illustrativemathematics.org/content-standards/HSA/SSE/B/4/tasks/805

F.BF.A.1b

A Sum of Functions

https://www.illustrativemathematics.org/content-standards/HSF/BF/A/1/tasks/230

F.BF.B.4a

Temperatures in degrees Fahrenheit and Celsius

https://www.illustrativemathematics.org/content-standards/HSF/BF/B/4/tasks/501

F.LE.A.4 Newton's Law of Cooling http://tasks.illustrativemathematics.org/content-sta ndards/HSF/LE/A/4/tasks/382

Mid Chapter Quizzes
End of Chapter Assessments
End of Unit Common Assessments

Stage 3: Learning Plan

Learning Opportunities/Strategies:

Lesson 5.1 – operations with functions add and subtract functions, multiply and divide functions, create a function,

Lesson 5.2 – composition of functions evaluate and perform compositions of functions, apply compositions of functions to real world problems

Lesson 5.3 – inverse functions and relations find and graph an inverse, find inverses with restricted domains, verify that two functions are inverses

Lesson 5.4 – graphing square root functions identify domain and range, graph square root functions, use graphs to analyze square root functions, find the inverse of power functions

Resources:

Glencoe Algebra 2 Textbook (Chapters 5 and 6)

 IXL

Delta math

Edulastic

Kahoot

Classkick

NJSLA Digital Library

Khan Academy

Lesson Presentations and Videos

Graphing Calculator

Desmos

Google Apps for Education

LGBT and Disabilities Resources:

- LGBTQ-Inclusive Lesson & Resources by Garden State Equality and Make it Better for Youth
- LGBTQ+ Books

DEI Resources:

- <u>Learning for Justice</u>
- GLSEN Educator Resources
- Supporting LGBTQIA Youth Resource List

Lesson 5.5 – graphing cube root functions identify attributes of cube root functions, graph cube root functions, find the inverse of cubic functions

Lesson 5.6 – solving radical equations Solve radical equations, solve a cube root equation, solve a radical equation

Lesson 6.1 – graphing exponential functions graph exponential growth functions, graph exponential decay functions, graph transformations

Lesson 6.2 – solving exponential functions and inequalities

Solve exponential equations, write an exponential function, apply functions to compound interest, solve exponential inequalities

Lesson 6.3 – geometric sequences and series find the nth term, write an equation for the nth term, find geometric means, find the sum of a geometric series, find the sum in sigma notation, find the first term of a series

Lesson 6.4 – logarithms and logarithmic functions logarithmic to exponential form, exponential to logarithmic form, evaluate logarithmic expressions, graph logarithmic functions

Lesson 6.6 – properties of logarithms
Use the product property, quotient property, power
property of logarithms, solve equations using
properties of logarithms

Lesson 6.7 – common logarithms find common logarithms, solve logarithmic equations, solve exponential equations using logarithms, solve exponential inequalities using logarithms, change of base formula

Lesson 6.8 – natural logarithms

- Respect Ability: Fighting Stigmas, Advancing Opportunities
- NJDOE Diversity, Equity & Inclusion Educational Resources
- <u>Diversity Calendar</u>

Write equivalent expressions, simplify expressions with e and the Natural log, solve base e equations and inequalities, solve natural log equations and inequalities

Lesson 6.9 – solving logarithmic equations and inequalities Solve a logarithmic equation, solve a logarithmic inequality, solve inequalities with logarithms on each side

Lesson 6.10 – using logarithms to solve exponential problems Exponential decay problems, carbon dating, continuous exponential growth

Differentiation

*Please note: Teachers who have students with 504 plans that require curricular accommodations are to refer to Struggling and/or Special Needs Section for differentiation

High-Achieving	On Grade Level	Struggling Students	Special Needs/ELL
Students	Students		
Khan Academy Project based learning Tablets Challenging problems with higher degree of difficulty Higher order thinking questions Differentiation of pacing and activities Differentiation of learning strategies: visual, auditory, kinetic and cooperative Enrichment and extension Technology connection Practice assignments Puzzle time activities Record and practice journal	Tutoring Tables Graphic organizers Differentiation of learning strategies: visual, auditory, kinetic and cooperative Technology connection Practice Assignments Puzzle time activities Record and practice journal Differentiating the lesson activities Lesson tutorials Skills review handbook	Provide a highly structured, predictable learning environment Provide organizers/study guides Lessons designed to the style of learning that matches the student Cooperative Learning Positive reinforcement Announce test with adequate prep time Lessons presentation available on google classroom Frequent check for understanding Break down task into manageable units One-on-one instruction Tutoring Pair student with a high achieving student	Any student requiring further accommodations and/or modifications will have them individually listed in their 504 Plan or IEP. These might include, but are not limited to: breaking assignments into smaller tasks, giving directions through several channels (auditory, visual, kinesthetic, model), and/or small group instruction for reading/writing ELL supports should include, but are not limited to, the following:: Extended time Provide visual aids Repeated directions Differentiate based on proficiency Provide word banks Allow for translators, dictionaries
		otagont	

Unit Title: Unit 4: Rational Functions and Probability

Stage 1: Desired Results

Standards & Indicators:

A.REI.A.2

Solve simple rational and radical equations in one variable, and give examples showing how extraneous solutions may arise.

A.REI.D.11

explain why the x-coordinates of the points where the graphs of two equations y = f(x) and y = g(x) intersect are the solutions of the equations f(x) = g(x). Find the solutions using technology, make tables of values and include cases where the functions are linear, polynomial, rational, absolute value, exponential and logarithmic functions.

F.IF.B.4

for a function that models a relationship between two quantities, interpret key features of the graph and tables and sketch graphs given a verbal description of the relationship

S.IC.B.3

Recognize the purposes of and differences among sample surveys, experiments, and observational studies; explain how randomization relates to each.

S.IC.B.4

Use data from a sample survey to estimate a population mean or proportion; develop a margin of error through the use of simulation models for random sampling.

S.IC.B.5

Use data from a randomized experiment to compare two treatments; use simulations to decide if differences between parameters are significant.

S.IC.B.6

Evaluate reports based on data.

Career Readiness, Life Literacies and Key Skills			
Standard	Performance Expectations	Core Ideas	
9.4.12.CI.1	Demonstrate the ability to reflect, analyze, and use creative skills and ideas (e.g., 1.1.12prof.CR3a).	With a growth mindset, failure is an important part of success.	
9.4.12.CT.1	Identify problem-solving strategies used in the development of an innovative product or practice (e.g., 1.1.12acc.C1b, 2.2.12.PF.3).	Collaboration with individuals with diverse experiences can aid in the problem-solving process, particularly for global issues where diverse solutions are needed.	
9.4.12.GCA.1	Collaborate with individuals to analyze a variety of potential solutions to climate change effects and determine why some solutions (e.g., political. economic, cultural) may work better than others (e.g., SL.11-12.1., HS-ETS1-1, HS-ETS1-2, HS-ETS1-4,	Solutions to the problems faced by a global society require the contribution of individuals with different points of view and experiences.	

6.3.12.GeoGI.1, 7.1.IH.IPERS.6, 7.1.IL.IPERS.7, 8.2.12.ETW.3).

Central Idea/Enduring Understanding:

Chapter 7

Rational expressions are ratios of two polynomial expressions. Operations with rational expressions are similar to operations with fractions. The graphs of some rational functions have breaks in continuity and may have vertical and horizontal asymptotes. Rational equations can be solved as polynomial equations once the fractions are eliminated by multiplying by the LCD

Chapter 8

A statistic is a measure that describes a characteristic of a sample. The shape of a distribution of data can be symmetric, positively skewed, or negatively skewed. The mean and standard deviation or five-number summary can be used to describe or compare the distribution of sets of data. A probability distribution is a function that maps the sample space to the outcomes in the sample space. The normal distribution is a continuous, symmetric, bell-shaped distribution of a random variable.

Essential/Guiding Question:

At the end of the Unit, students should be able to answer the Essential Questions:

Chapter 7 – Why are graphs useful?

Chapter 8 - How can you effectively evaluate information? How can you use information to make decisions?

Content:

- 7.3 graphing reciprocal functions
- 7.4 graphing rational functions
- 7.5 variation functions
- 7.6 solving rational equations and inequalities
- 8.1 random sampling
- 8.2 using statistical experiments
- 8.3 population parameters
- 8.5 evaluating published data
- 8.6 normal distributions

Skills(Objectives):

determine properties of reciprocal functions

graph transformations of reciprocal functions

graph rational functions with vertical and horizontal asymptotes

graph rational functions with oblique asymptotes and point discontinuity

recognize and solve direct and joint variation problems

recognize and solve inverse and combined variation problems

solve rational equations and inequalities

distinguish among sample surveys, experiments and observational studies

make inferences about population parameters based on random samples of the population

collect and analyze data by conducting simulations of real life situations

use data to compare theoretical and experimental probabilities

use data from sample surveys to estimate population means or proportions

develop margins of error by using simulation models

evaluate reports based on data

identify and explain misleading uses of data

use the empirical rule to analyze normally distributed variables

apply the standard normal distribution and z-values

Interdisciplinary Connections:

Interdisciplinary connections are integrated in each unit with connections to the mathematical practices.

- 1. Make sense of problems and persevere in solving them
- 2. Reason abstractly and quantitatively
- 3. Construct viable arguments and critique the reasoning of others
- 4. Model with mathematics
- 5. Use appropriate tools strategically
- 6. Attend to precision
- 7. Look for and make use of structure
- 8. Look for and express regularity in repeated reasoning

Stage 2: Assessment Evidence

Performance Task(s):

S.IC.A.1

School Advisory Panel

https://www.illustrativemathematics.org/content-standards/HSS/IC/A/1/tasks/186

S.IC.A.2

Sarah, the chimpanzee

https://www.illustrativemathematics.org/content-standards/HSS/IC/A/2/tasks/1099

S.IC.B.3

Strict Parents

https://www.illustrativemathematics.org/content-standards/HSS/IC/B/3/tasks/122

F.IF.B.4 Influenza Epidemic

http://tasks.illustrativemathematics.org/content--standards/HSF/IF/B/4/tasks/637

Other Evidence:

Written and Online Assignments
Exit Cards
Mid Chapter Quizzes
End of Chapter Assessments
End of Unit Common Assessments

Stage 3: Learning Plan

Learning Opportunities/Strategies:

Lesson 7.3 – graphing reciprocal functions determine limitations on a domain, determine properties of reciprocal functions, graph transformations, write equations to represent real world problems

Lesson 7.4 – graphing rational functions graph with no horizontal asymptote, use graphs of rational functions, determine oblique asymptotes, graph with point discontinuity

Lesson 7.5 – variation functions
Find direct variation and joint variation, write and solve an inverse and combined variation

Lesson 7.6 – solving rational equations and inequalities

solve a rational equation, solve a mixture problem, solve a distance problem, solve a rational inequality

Lesson 8.1 – random sampling classify study types, make an inference about population

Lesson 8.2 – using statistical experiments design a simulation by using random numbers, conduct and evaluate a simulation, conduct and summarize data from a simulation

Lesson 8.3 – population parameters use data to estimate population mean, calculate margin of error, use margin of error to find sample size

Lesson 8.5 – evaluating published data evaluate a report, identify misleading uses of data

Lesson 8.6 – normal distributions use the empirical rule to analyze data and distributions, use z-values to locate position, find probabilities

Resources:

Glencoe Algebra 2 Textbook (Chapters 7 and 8)

IXL

Delta math

Edulastic

Kahoot

Classkick

NJSLA Digital Library

Khan Academy

Lesson Presentations and Videos

Graphing Calculator

Desmos

Google Apps for Education

LGBT and Disabilities Resources:

- <u>LGBTQ-Inclusive Lesson & Resources by Garden</u>
 <u>State Equality and Make it Better for Youth</u>
- LGBTQ+ Books

DEI Resources:

- Learning for Justice
- GLSEN Educator Resources
- Supporting LGBTQIA Youth Resource List
- Respect Ability: Fighting Stigmas, Advancing Opportunities
- NJDOE Diversity, Equity & Inclusion Educational Resources
- Diversity Calendar

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Pacing Guide

Algebra II Honors	Glencoe Algebra II	MAJOR
UNIT 1 Equations, Relations	CHAPTERS	A.REI.D.11
and Functions (18 Days)	1: (11 Days)	F.IF.B.4
	2: (7 Days)	F.IF.B.6
		A.CED.A1
		F.IF.C.7
		F.IF.C.9
UNIT 2 Quadratic and	CHAPTERS	A.APR.B.2
Polynomial Functions (22	3: (10 Days)	A.APR.B.3
Days)	4: (12 Days)	A.REI.D.11-12
		A.SSE.A.2
		F.IF.B.4
		F.IF.B.6
		A.APR.D.6
		A.CED.A.1
		F.IF.C.8
		F.IF.C.9
		N.Q.A.2
END OF MP		
UNIT 3 Radical, Exponential	CHAPTERS	A.REI.2
and Logarithmic Functions	5: (6 Days)	A.REI.D.11
(20 Days)	6: (14 Days)	A.SSE.A.2
		A.SSE.B.4
		F.BF.A.1
		F.IF.B.4
		F.IF.C.7
		F.IF.C.8
		F.IF.C.9
		F.LE.A.4
		N.RN.2

UNIT 4 Rational Functions &	CHAPTERS	A.REI.2
Probability (18 Days)	7: (9 Days)	A.REI.D.11
	8: (9 Days)	F.IF.B.4
		S.IC.B.3
		S.IC.B.4
		S.IC.B.5
		S.IC.B.6
END OF MP		