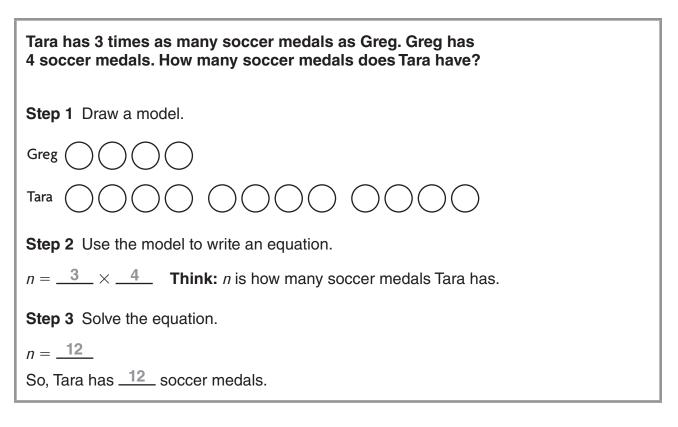
### **Algebra** • Multiplication Comparisons



#### Draw a model and write an equation.

- **1.** 4 times as many as 7 is 28. **2.** 16 is 8 times as many as 2.

**3.** 3 times as many as 6 is 18. **4.** 10 is 2 times as many as 5.

Name .

# **Multiplication Match-Up**

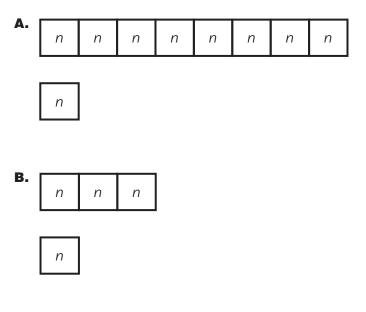
#### Match each word problem to a model. Write the equation and solve.

 Angie has 36 coins. This is 4 times as many coins as Scott has. How many coins does Scott have?

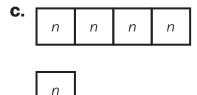
2. Cindy bought 20 stamps. This is

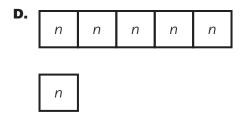
that Yoshi bought. How many

5 times the number of postcards



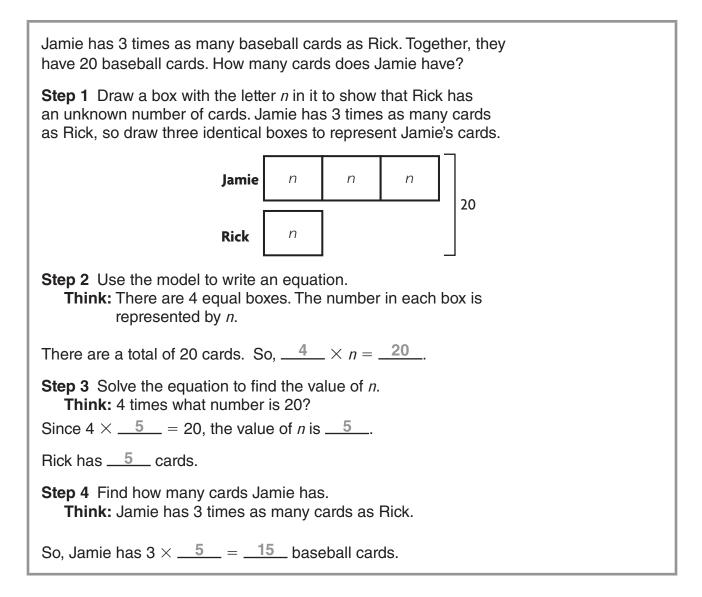
- postcards did Yoshi buy?
- Jessica has 48 stickers. This is 8 times as many stickers as Taylor has. How many stickers does Taylor have?
- 4. Joshua picked 24 apples. This is 3 times the number of apples that Carly picked. How many apples did Carly pick?





**5. Stretch Your Thinking** Write four comparison sentences for the product 12.

# **Algebra • Comparison Problems**



#### Draw a model. Write an equation and solve.

 Maddie has 2 times as many stickers on her notebook as Meg. Together, they have 15 stickers. How many stickers are on Maddie's notebook?
 How many more stickers are on Maddie's notebook than on Meg's notebook?

#### Lesson 2.2 Enrich

# **Mixed Models**

#### Solve each problem.

- Together, Tom and Max have 72 football cards. Tom has 2 more than 4 times as many cards as Max has. How many football cards does Tom have?
- 2. Naomi has 50 red beads and white beads. The number of red beads is 1 more than 6 times the number of white beads. How many red beads does Naomi have?

- Javier rode his bike for a total of
  41 minutes. Before lunch, he rode for
  1 minute less than 5 times the number of minutes he rode after lunch. How many minutes did Javier ride before lunch?
- 4. Marnie practiced her basketball dribbling. After two tries, she had bounced the ball 88 times. On the second try, she had 2 fewer bounces than 8 times the number of bounces she had on the first try. How many bounces did she have on the second try?
- Write Math How can a multiplication model help you solve Problem 1?

### Multiply Tens, Hundreds, and Thousands

You can use a pat	ttern to multiply with tens, hundreds, and thousands.
Count the number	of zeros in the factors.
4 × 6 = 24	$\leftarrow$ basic fact
4 × 6 <u>0</u> = 24 <u>0</u>	← When you multiply by tens, the last digit in the product is 0.
$4 \times 600 = 2,400$	← When you multiply by hundreds, the last <u>two</u> digits in the product are 0.
4 × 6, <u>000</u> = 24, <u>000</u>	<u>0</u> ← When you multiply by thousands, the last <u>three</u> digits in the product are 0.
When the basic fac in the final product	ct has a zero in the product, there will be an extra zero :
$5 \times 4 = 20$ , so 5 $\times$	4,000 = 20,000

#### Complete the pattern.

Chapter Resources © Houghton Mifflin Harcourt Publishing Company	2-9		Reteach
=		=	
= ł	undreds	= t	housands
<b>5.</b> 7 × 300 = 7 ×	hundreds 6.	5 × 8,000 = 5 ×	_ thousands
Find the product.			
6 × 6,000 =	_	4 × 7,000 =	
6 × 600 =		4 × 700 =	
6 × 60 =		4 × 70 =	
<b>3.</b> 6 × 6 = 36	4.	4 × 7 = 28	
9 × 2,000 =	-	8 × 4,000 =	
9 × 200 =		8 × 400 =	
9 × 20 =		8 × 40 =	
<b>1.</b> 9 × 2 = 18	2.	8 × 4 = 32	

# **Multiplication Inequalities**

Write  $\langle , \rangle$ , or = for each ().

- **1.**  $7 \times 60 \bigcirc 400$  **2.**  $700 \bigcirc 90 \times 8$
- **3.** 3 × 800 2,500 **4.** 2,000 400 × 5
- **5.** 8 × 6,000 40,000 **6.** 3 × 9,000 39,000
- **7.**  $6 \times 900 \bigcirc 700 \times 8$  **8.**  $8 \times 3,000 \bigcirc 6,000 \times 4$
- **9.**  $9 \times 4,000 \bigcirc 6,000 \times 6$  **10.**  $800 \times 9 \bigcirc 3,000 \times 3$
- **11.** (Write Math >> Explain how you found the answer in Exercise 10.

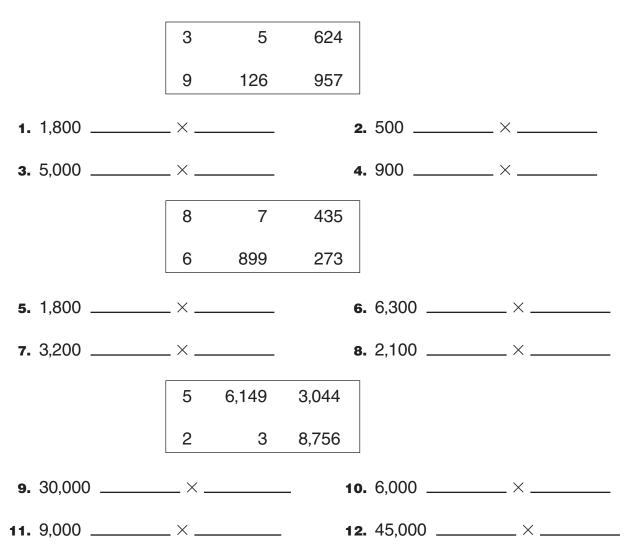
### **Estimate Products**

Round the greater factor. Then use	e mental math to estimate the product.
6 × 95	
Step 1 Round 95 to the nearest ten	. 95 rounds to <b>100</b> .
Step 2 Use patterns and mental ma	ath. $6 \times 1 = 6$
	$6 \times 10 = 60$
	6 × 100 = 600
Find two numbers the exact answe	er is between.
7 × 759	
<b>Step 1</b> Estimate by rounding to the I hundred.	esser <b>Step 2</b> Estimate by rounding to the greater hundred.
7 × 759 Think: 7 × 7 = 49 7 × 70 = 490 7 × 700 = 4,900 7 × 700 = 4,900	7 × 800 = 5,600
So, the product is between 4,900	and 5,600.
stimate the product by rounding.	
	× 29 <b>3.</b> 4 × 703

Estimate the product the exact answer is be	by finding two numbers etween.	
4. $3  imes 558$	<b>5.</b> 7 × 252	<b>6.</b> 8 × 361

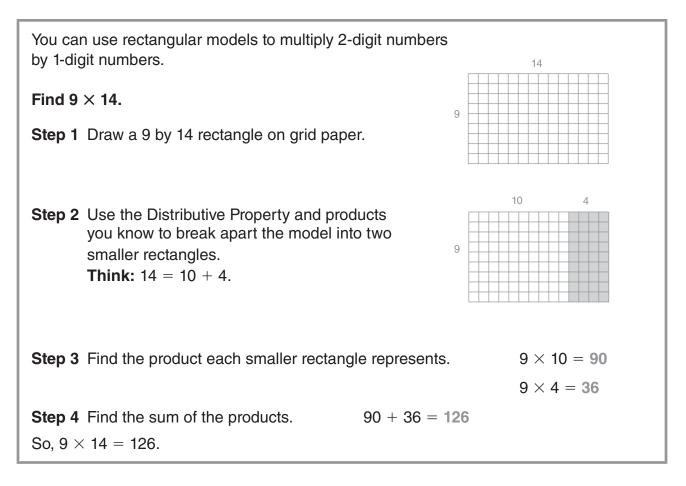
### **Find the Unknown Factors**

Choose two factors from the box to make the estimated product. You may use the factors more than once.

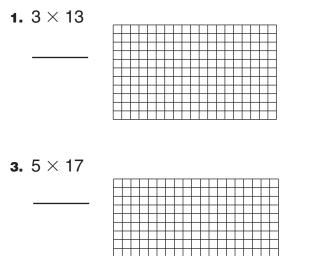


**13. Stretch Your Thinking** Two factors have an estimated product of 10,000. One of these factors is a single digit. What two factors could they be? **Explain** your thinking.

# **Multiply Using the Distributive Property**



#### Model the product on the grid. Record the product.



**2.**  $6 \times 16$ 

									1

**4.** 4 × 14

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# **Shading the Grids**

Use the Distributive Property. Shade and label each grid.

1. Show 3 imes 28 in two different ways.

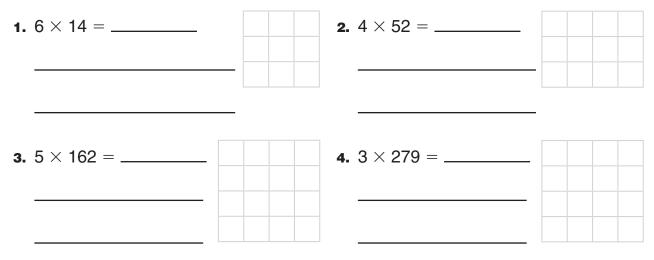
**2.** Show 4  $\times$  23 in two different ways.

**3. Stretch Your Thinking** Find the partial products for one of your grids in Exercise 1. Then use the Distributive Property to find the product  $3 \times 28$ .

# **Multiply Using Expanded Form**

You can use expanded form or a model to find products. Multiply.  $3 \times 26$ Think and Write Use a Model Step 1 Write 26 in expanded form. Step 1 Show 3 groups of 26. 26 = 20 + 6<u>00000 mmmnmmn</u>000000  $3 \times 26 = 3 \times (20 + 6)$ **Step 2** Use the Distributive Property. Step 2 Break the model into tens and ones.  $3 \times 26 = (3 \times 20) + (\underline{3} \times \underline{6})$ **Step 3** Multiply the tens. Multiply the ones.  $(3 \times 2 \text{ tens})$   $(3 \times 6 \text{ ones})$  $3 \times 26 = (3 \times 20) + (3 \times 6)$  $(3 \times 20)$  $(3 \times 6)$ = <u>60</u> + <u>18</u> 60 18 60 +18**Step 4** Add the partial products. **Step 3** Add to find the total product. 78 <u>60</u> + <u>18</u> = <u>78</u> So, 3 × 26 = <u>78</u>.

#### Record the product. Use expanded form to help.



### **Expanded Form Match-Up**

Write the multiplication expression for each expanded form. Then match the multiplication expression with its product.

1. $(7 \times 900) + (7 \times 80) + (7 \times 7)$	<b>A.</b> 15,144
	<b>B.</b> 7,065
<b>2.</b> $(3 \times 5,000) + (3 \times 40) + (3 \times 8)$	<b>c.</b> 15,720
<b>3.</b> (8 × 900) + (8 × 2)	<b>d.</b> 6,909
	<b>E.</b> 16,224
<b>4.</b> (4 × 3,000) + (4 × 900) + (4 × 60) + (4 × 2)	<b>F.</b> 15,848
	<b>G.</b> 7,360
<b>5.</b> (2 × 7,000) + (2 × 800) + (2 × 6)	н. 7,216
6. $(9 \times 700) + (9 \times 80) + (9 \times 5)$	<b>I.</b> 15,612
	<b>J.</b> 14,172

### **Multiply Using Partial Products**

Use partial products to multiply.	
Multiply. 7 $ imes$ \$332	
Step 1 Estimate the product.	332 rounds to 300; $7 \times $300 = \frac{$2,100}{.}$
<b>Step 2</b> Multiply the 3 hundreds, or 300, by 7.	$\frac{\$332}{\times 7}$ or $\frac{\$300}{\times 7}$ \$2,100
Step 3 Multiply the 3 tens, or 30, by 7.	$\frac{332}{\times 7}$ or $\frac{\times 7}{3210}$
Step 4 Multiply the 2 ones, or 2, by 7.	$ \xrightarrow{\$332}_{\times \underline{7}} \text{ or } \xrightarrow{\$2}_{\times \underline{7}} $
Step 5 Add the partial products.	2,100 + 210 + 14 =
So, 7 $\times$ \$332 = \$2,324. Since \$2,324 is to the estimate of \$2,100, it is reasonable	

#### Estimate. Then record the product.

1. Estimate:	<b>2.</b> Estimate:	<b>3.</b> Estimate:
181 <u>× 2</u>	156 <u>× 4</u>	\$210 <u>× 5</u>
<b>4.</b> Estimate:	<b>5.</b> Estimate:	<b>6.</b> Estimate:
$303 \times 6$	\$427 <u>× 2</u>	$367 \times 5$

# **Shaping Factors**

Choose one number from a circle and another number from a triangle. Then use these two numbers to write a number sentence that is true. You can use numbers more than once.

1.	Find the least product.	8	5
2.	Find the greatest product.		
3.	Find the product closest to 1,050.	\$421	2
4.	Find a product with an 8 in the ones place.	\$583	4
5.	Find the greatest product ending in 25.	(\$300)	
6.	Find a product between 1,500 and 1,700.	149	125
7.	Find a product that contains only the digits 2 and 9.	$\wedge$	$\frown$
8.	Find the product with three zeros.	9	(120)
9.	Find the product closest to 500.	\$374	7
10.	Find the product closest to 2,000.	$\checkmark$	

### **Multiply Using Mental Math**

Use addition to break apart the larger factor.	Use subtraction to break apart the larger factor.
Find 8 × 214.	Find 6 $ imes$ 298.
<b>Think:</b> 214 = 200 + 14	<b>Think:</b> 298 = 300 - 2
$8 \times 214 = (8 \times 200) + (8 \times 14)$	$6 \times 298 = (6 \times 300) - (6 \times 2)$
= <u>1,600</u> + <u>112</u>	= <u>1,800</u> – <u>12</u>
= <u>1,712</u>	= <u>1,788</u>
Use halving and doubling.	When multiplying more than two numbers, use the Commutative Property to change the order of the factors.
Find 14 $ imes$ 50.	Find 2 $\times$ 9 $\times$ 50.
Think: 14 can be evenly divided by 2.	<b>Think:</b> $2 \times 50 = 100$
$14 \div 2 = \underline{7}$	$2 \times 9 \times 50 = 2 \times \underline{50} \times 9$
7 × 50 = <u>350</u>	= <u>100</u> × 9
2 × 350 = <u>700</u>	= <u>900</u>

Find the product. Tell which strategy you used.

**1.**  $5 \times 7 \times 20$  **2.**  $6 \times 321$ 

**3.**  $86 \times 50$ 

4.  $9 \times 399$ 

# Multiply by 11 Mentally

To find the product of a two-digit number and 11, add the digits in the two-digit number and write the sum between the two digits. If the sum is greater than 9, write the *last* digit of the sum between the two digits. Then add 1 to the *first* digit.

<b>Example 1:</b> Multiply $25 \times 11$ .	<b>Example 2:</b> Multiply 59 $\times$ 11.
Add the digits in 25: $2 + 5 = 7$	Add the digits in 59: $5 + 9 = 14$
Place the sum, 7, between 2 and 5.	Place the last digit, 4, between 5 and 9.
So, $25 \times 11 = 275$ .	Add 1 to the first digit: $5 + 1 = 6$
	So, $59 \times 11 = 649$ .

#### Find the product.

<b>1.</b> 17 × 11	<b>2.</b> 32 × 11	<b>3.</b> 45 × 11
	- 67 × 11	
<b>4.</b> 39 × 11	<b>5.</b> 67 × 11	<b>6.</b> 89 × 11

**7. Stretch Your Thinking** Find a way to multiply  $354 \times 11$  mentally. Describe your method and show that it works.

### Problem Solving • Multistep Multiplication Problems

# Use the strategy *draw a diagram* to solve a multistep multiplication problem.

Amy planted 8 rows with 18 tulips in each row. In each of the 4 middle rows, there are 4 red tulips. All of the other tulips are yellow. How many of the tulips are yellow tulips?

Read the Problem	Solve the Problem	
What do I need to find?	I drew a diagram for each color of tulip.	
I need to find the total number of <u>yellow</u> tulips.	18 tulips	
What information do I need to use?	$\begin{array}{c c} \mathbf{L} \\ \mathbf{\nabla}_{\mathbf{V}} \\ \end{array} \\ \end{array} \\ \hline \begin{array}{c} \mathbf{R} \\ \mathbf{R} \\$	
There are <u>8</u> rows of tulips with <u>18</u> tulips in each row.	4 tulips	
There are <u>4</u> rows of tulips with <u>4</u> red tulips in each row.	Next, I found the number in each section.           All Tulips         Red Tulips	
How will I use the information?	$8 \times 18 = 144 \qquad 4 \times 4 = 16$	
I can <u>multiply</u> to find the total number of tulips and the number of red tulips.	Last, I subtracted the number of red tulips from the total number of tulips.	
Then I can <u>subtract</u> to find the number of yellow tulips.	144 - 16 = 128 So, there are 128 yellow tulips.	

- A car dealer has 8 rows of cars with 16 cars in each row. In each of the first 3 rows, 6 are used cars. The rest of the cars are new cars. How many new cars does the dealer have?
- 2. An orchard has 4 rows of apple trees with 12 trees in each row. There are also 6 rows of pear trees with 15 trees in each row. How many apple and pear trees are in the orchard?

# 2-Digit Roses

#### Draw a diagram to solve the problem.

A rose garden has 8 rows of 26 rose bushes each. In each of the first 5 rows, 7 bushes have pink roses. In each of the first 3 rows, 12 bushes have yellow roses. The rest of the bushes have red roses. How many bushes have red roses?

Read the Problem	Solve the Problem
What do I need to find?	Draw a diagram and do your work here.
I need to find the number of bushes with roses.	
What information do I need to use?	
In the entire garden, there are rows with bushes in each row.	
There are rows with pink bushes in each row.	I found the total number of rose bushes.
There are rows with yellow bushes in each row.	pink rose bushes.
How will I use the information?	of yellow rose bushes.
I can to find the total number of bushes, the number of pink rose bushes, and the number of yellow rose bushes.	

1. What else do you need to do to solve the problem?

**2. Stretch Your Thinking** Give at least two reasons why drawing a diagram is helpful when solving a problem.

### **Multiply 2-Digit Numbers with Regrouping**

Use place value to multiply with regrouping.			
Multiply. 7 $ imes$ 63			
Step 1 Estimate the product.	7 × 60 = <b>420</b>		
<b>Step 2</b> Multiply the ones. Regroup 21 ones as <b>2</b> tens 1 one. Record the 1 one below the ones column and the <b>2</b> tens above the tens column.			
$7 \times 3 \text{ ones} = 21 \text{ ones}$	2		
<b>Step 3</b> Multiply the tens. Then, add the regrouped tens. Record the tens.	$\begin{array}{rr} 63 \\ \underline{\times 7} \\ 441 \end{array} \qquad \begin{array}{r} 44 \text{ tens} = 4 \text{ hun} \\ 4 \text{ tens} \end{array}$		
$7 \times 6$ tens = 42 tens			
Add the 2 regrouped tens.			
42 tens + 2 tens = <b>44 tens</b>			
So, $7 \times 63 = 441$ . Since 441 is close to the estimate of 420, it is reasonable.			

#### Estimate. Then record the product.

1. Estimate:	<b>2.</b> Estimate:	<b>3.</b> Estimate:	4. Estimate:
42	\$98	37	\$54
× 6	<u>× 6</u>	<u>× 8</u>	<u>× 9</u>
<b>5.</b> Estimate:	<b>6.</b> Estimate:	<b>7.</b> Estimate:	<b>8.</b> Estimate:
37	93	86	59
_× 5	<u>× 4</u>	<u>× 9</u>	× 7

# **Regrouping Review**

# Each multiplication problem below was solved using partial products. Some errors were made. Multiply using regrouping to check each answer. Describe any errors that you find.

1. Partial product	Regrouping	2. Partial product	Regrouping
$     \begin{array}{r}       72 \\       \times 8 \\       26 \\       + 560 \\       586     \end{array} $	72 <u>× 8</u>		65 × 9
Did you find any errors? If so, describe.		Did you find any error	s? If so, describe.
3. Partial product	Regrouping	4. Partial product	Regrouping
$ \begin{array}{r}     36 \\     \times 5 \\     11 \\     + 150 \\     161 \end{array} $	36 <u>× 5</u>	$ \begin{array}{r} 47 \\ \times 4 \\ 28 \\ + 16 \\ 44 \end{array} $	47 <u>× 4</u>
Did you find any errors? If so, describe.		Did you find any error	s? If so, describe.

- **5. Stretch Your Thinking** Compare the factors and the product in Exercise 4. What information does this give you?
- **6. Write Math Explain** how you can use partial products to check products you found with regrouping.

### Multiply 3-Digit and 4-Digit Numbers with Regrouping

When you multiply 3-digit and 4-digit numbers, you may need to regroup.			
Estimate. Then find the product. $\$1,324$ $\times 7$			
<b>Step 1</b> Estimate the product. $$1,324$ rounds to $$1,000$ ; $$1,000 \times 7 = $7,000$ .			
Step 2 Multiply the 4 ones by 7. $\$1,324$ Regroup the 28 ones as 2 tens 8 ones. $\times$ 8			
Step 3 Multiply the 2 tens by 7.12Add the regrouped tens.\$1,324Regroup the 16 tens as 1 hundred 6 tens. $\times \frac{7}{68}$			
Step 4 Multiply the 3 hundreds by 7.2 1 2Add the regrouped hundred.\$1,324Regroup the 22 hundreds as 2 thousands× 72 hundreds.268			
Step 5 Multiply the 1 thousand by 7. $2 12$ \$1,324 $\times 7$ \$9,268			
So, $7 \times \$1,324 = \$9,268$ . Since $\$9,268$ is close to the estimate of $\$7,000$ , the answer is <b>reasonable</b> .			

#### Estimate. Then find the product.

1. Estimate:	<b>2.</b> Estimate:	<b>3.</b> Estimate:	<b>4.</b> Estimate:
3,184 × 2	$\frac{\$828}{\times 4}$	2,637 $\times$ 5	

# **Multiplication Mystery**

There's something mysterious in the water off the coast of Florida. To discover what it is, find the products and use the decoder below. The first letter has been done for you.

1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26
A	B	C	D	Ε	F	G	Η		J	K	L	Μ	Ν	0	Ρ	Q	R	S	Τ	U	V	W	X	Υ	Ζ

<b>1. Letter 1:</b> 2 × 6,532	<b>2. Letter 2:</b> 5 × 245	<b>3.Letter 3:</b> 3 × 4,893	<b>4. Letter 4:</b> 7 × 198
Answer: <u>13,064</u>	Answer:	Answer:	Answer:
Code: Use the ten thousands digit and the thousands digit. 13 Letter: M	Code: Use the thousands digit.	Code: Use the ten thousands digit and the thousands digit. Letter:	Code: Use the thousands digit.
<b>5. Letter 5:</b> 6 × 3,411	<b>6. Letter 6:</b> $4 \times 129$	<b>7. Letter 7:</b> 8 × 730	
Answer:	Answer:	Answer:	
Code: Use the ten thousands digit and the thousands digit.	Code: Use the hundreds digit.	Code: Use the thousands digit.	
Letter:	Letter:	Letter:	

IT'S A <u>M</u>\_\_\_\_!

**8.** The product of 5 and another number has the code for E in its ones place. What digit could be in the ones place of the other number? **Explain**.

**9. (Write Math**) Is the product of a 4-digit number and a 1-digit number always a 5-digit number? **Explain**.

### Algebra • Solve Multistep Problems Using Equations

The **Order of Operations** is a special set of rules which gives the order in which calculations are done in an expression. First, multiply and divide from left to right. Then, add and subtract from left to right.

Use the order of operations to find the value of *n*.

 $6 \times 26 + 3 \times 45 - 11 = n$ 

Step 1 Circle the first multiplication expression in the equation.

 $6 \times 26 + 3 \times 45 - 11 = n$ 

Step 2 Multiply  $6 \times 26$ .

<u>156</u> + 3 × 45 - 11 = n

Step 3 Circle the next multiplication expression in the equation.

 $156 + 3 \times 45 - 11 = n$ 

**Step 4** Multiply  $3 \times 45$ .

156 + <u>135</u> − 11 = *n* 

**Step 5** There are no more multiplication or division expressions. Circle the first addition expression in the equation.

(156 + 135) - 11 = n

Step 6 Add 156 + 135.

<u>291</u> – 11 = *n* 

Step 7 Subtract 291 - 11.

<u>280</u> = *n* 

#### Find the value of *n*.

**1.** 
$$5 \times 43 + 9 \times 24 + 25 = n$$

**2.**  $7 \times 29 + 4 \times 46 - 56 = n$ 

\_\_\_\_\_ = *n* 

\_\_\_\_\_ = *n* 

### **Same Answer Multistep**

Find the value of *n* for each exercise. Then identify the exercises that have the same answer.

- **1.**  $6 \times 36 + 3 \times 37 + 57 = n$ **2.**  $8 \times 47 + 2 \times 29 - 80 = n$ \_\_\_\_\_ = *n* \_\_\_\_\_ = *n* **3.**  $7 \times 45 + 4 \times 19 - 17 = n$ **4.**  $7 \times 56 + 2 \times 12 - 52 = n$ \_\_\_\_\_ = *n* \_\_\_\_\_ = *n* **5.**  $5 \times 52 + 6 \times 12 + 42 = n$ **6.**  $9 \times 32 + 4 \times 28 - 16 = n$ ----= n $_{-----} = n$ **7.**  $4 \times 46 + 3 \times 61 + 17 = n$ **8.**  $9 \times 39 + 2 \times 19 - 15 = n$ \_\_\_\_\_ = *n* \_\_\_\_\_ = *n* **9.**  $2 \times 98 + 8 \times 16 + 30 = n$ **10.**  $3 \times 75 + 4 \times 23 + 47 = n$  $_{-----} = n$  $_{-----} = n$
- Which exercise(s) have the same answer as Exercise 1?
- 12. Which exercise(s) have the same answer as Exercise 2? \_\_\_\_\_
- 13. Which exercise(s) have the same answer as Exercise 3? \_\_\_\_\_
- **14. Stretch Your Thinking** What statement can you make about the equations in Exercise 4 and Exercise 10? **Explain**.